

Public Debt and Interest Rates*

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Abstract

U.S. public debt has more than doubled over the past 25 years, potentially posing consequences for fiscal and monetary policy through its effect on interest rates. Standard theory predicts that higher debt crowds out productive capital, pushing rates up, but existing empirical estimates are typically static and ignore how the level of existing debt along with the composition and timing of debt-financed policies influence these effects. Using a heterogeneous agent life cycle model that is richly calibrated to U.S. household behavior, we show that there is significant variation in the dynamic interest rate responses across different debt-financed policies. Debt-financed transfers to households are partially saved, dampening the immediate effect on interest rate effects from crowding out, while debt from government consumption produces a larger immediate rate increase. Furthermore, the effect of debt on interest rates is amplified at higher baseline levels of debt. In order to quantify the dynamic effects on interest rates from the accumulated debt over the last several decades, we feed into the model the observed post-2000 debt and fiscal policy paths. We find the debt will eventually lead to a 180 basis point increase in the interest rate, of which only half has materialized to date and the remainder phases in over next 30 years. Critically, debt accumulated to date will provide significant upward pressure on interest rates going forward. These results highlight that accurately capturing the effects of public debt on interest rates requires incorporating dynamics along with the full path and composition of policy over history.

Keywords: Government Debt; Life Cycle; Heterogeneous Agents; Incomplete Markets

JEL Codes: H6, E21, E6

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1 Introduction

As U.S. public debt has more than doubled over the past 25 years, there has been renewed interest in understanding its economic effects.¹ A central prediction of standard theory is that an increase in public debt crowds out the productive capital stock and therefore raises interest rates. With current debt already incurring roughly \$1 trillion in annual servicing costs, empirical estimates of how interest rates respond to additional public debt are essential for projecting future service costs and assessing debt sustainability.² Such estimates are not only critical for fiscal planning but also for monetary policy, which relies on the equilibrium interest rate and its response to shocks as a key input to determining an appropriate policy.³ However, for all of their importance, existing empirical estimates of the relationship between interest rates and public debt are typically narrow in scope, abstracting from the existing level of debt, the composition of the debt-financed policies that give rise to the increase in debt, and from the timing of the effects on interest rates. Thus, to the detriment of policy-making, the existing empirical approach likely provides an incomplete characterization of the dynamic interest rate effects from these debt-financed fiscal policies that have starkly increased the debt in recent decades.

In this paper, we measure the distinct dynamic path of the interest rate response to a set of different fiscal policies that increase public debt, using a quantitative heterogeneous agent life-cycle model that replicates a rich set of empirical observations about household behavior in the cross-section and aggregate of the U.S. economy. Considering a set of fiscal policies that each increase public debt by the same amount, we find that each of the policies eventually lead to the same increase in interest rates in the long run. However, the initial response of the interest rate and the subsequent

¹After stabilizing in the 1990s at 40% as a share of GDP, U.S. public debt has grown steeply to its current size of 100% of GDP. The Congressional Budget Office projects that, under current law, debt will rise to 155% of GDP by 2055, while the Committee for a Responsible Fiscal Budget projects debt will rise to 120% of GDP by 2035.

²See seminal contributions from [Gale and Orszag \(2004\)](#), [Engen and Hubbard \(2004\)](#), and [Laubach \(2009\)](#), and recent updates in [Gamber and Seliski \(2019\)](#) and [Plante et al. \(2025\)](#). The CBO recently noted the importance of this relationship in their projections and revisited their estimated assumption for the long run elasticity (see [Neveu and Schafer \(2024\)](#)). Moreover, most studies examining debt sustainability incorporate or discuss how government debt increases borrowing rates thus putting further pressure on debt sustainability (for example, see [Blanchard \(2022\)](#), [Edelberg et al. \(2025\)](#), [Dynan and Elmendorf \(2025\)](#), and [Blanchard \(2019\)](#)). Relatedly, others have noted the increase in household borrowing costs associated with rising rates from government debt (see [Gupta \(2026\)](#)).

³In particular, [Woodford \(2003\)](#) characterizes monetary policy as a central bank's setting of the short term deviations between the federal funds rate and the equilibrium interest rate in order to achieve its stabilization goal. As described in [Barsky et al. \(2014\)](#), the interest rate in our model that equates real savings and investment is consistent with the Wicksellian or natural rate of interest in the flexible price model.

transition path to the new equilibrium rate is quite different across policies. For example, some policies lead to essentially no initial change and the subsequent upward pressure on interest rates takes several decades to fully materialize. In contrast, other policies cause the interest rate to initially jump and overshoot its long run value before subsequently falling back toward its new equilibrium rate. Moreover, the long run interest rate elasticity is increasing with the initial level of debt. Thus, these results imply that measuring the effect of previously accumulated debt on both current and future interest rates requires knowing not only the current level of debt – it requires knowing both the composition of policies that generated the debt and when those policies were enacted. Accordingly, we simulate the model economy with observed paths for debt due to changes in fiscal policies since 2000 in order to measure the effect on interest rates to date along with the implications for the future path for the interest rate. We find that already-accumulated debt will eventually boost the interest rate by 180 basis points, but only about half of the effect has phased into long rates so far, implying that the current debt will still lead to 80 basis points of upward pressure on interest rates over the next several decades.

In order to investigate why different policies induce distinct interest rate dynamics, we start by constructing transition paths after three different shocks that increase debt by the same amount and converge to a common steady state: (i) a one-period increase in government purchases, (ii) a one-period increase in government transfers to households, (iii) and a one-period reduction in income tax rates. All three fiscal shocks yield an interest rate elasticity of 1.6 basis points with respect to a 1 percentage point increase in public debt between the initial and new steady states that are common to each. However, we find substantial variation in interest rate responses of varying maturities and over time that arise from distinct transitional dynamics following each of the fiscal shocks.⁴

The different dynamic responses are the result of two channels by which a fiscal policy affects the interest rate. First, holding household savings constant, public debt directly crowds out productive capital thus raising the interest rate. We refer to this as the *direct crowd-out channel*. Second, however, household savings decisions need not be held constant. For example, if the deficit shock funds a windfall for households—such as a temporary tax cut or transfer payment—it can lead households to initially save more, thereby offsetting some of reduction in productive capital and inducing a smaller increase in interest rates. We refer to this as the *savings channel*.

While the direct crowd-out channel has the same immediate and stable impact on

⁴We consider both spot rates and longer run yields, which are determined by the path of the one period spot interest rates over each transition from a fiscal policy change.

spot interest rates for any fiscal policy, the savings channel's effect varies both with policy type and along the transition, leading to the substantial variation in the interest rate response to debt policies. For example, when the debt finances government expenditures, the savings channel is essentially zero at the onset of the shock since households do not directly receive resources from the increase in debt. The initial large increase in the interest rate from the direct crowd out channel leads households to save more over time offsetting some of the reduction in productive capital and leading to a smaller increase in the interest rate in the long run. Thus, with no initial offset to the direct crowd out channel, the spot interest rate increases even more at the onset of the shock and overshoots the eventually higher steady state rate. All told, the longer term yield at the time of the shock is even higher than the new steady state interest rate leading to a larger elasticity of 2 bp for a 1 pp increase in debt on the ten year yield. Moreover, after the initial boost, this shock leads to downward pressure on long rates.

In contrast, when the debt finances a lower income tax rate or lump sum transfers to households for one period, households receive resources. Households respond by saving most of the windfall, which strengthens the savings channel at the onset of the shock. The saving channel and direct crowd out channel mostly offset and there is little change in the spot interest rate at the onset of the transition. Over time, households spend down some of the windfall reducing the strength of the savings channel such that the direct crowd out channel dominates and the spot rate rises. All told, the 10 year interest rate elasticity at the time of the shock is much smaller. However, after the initial small effect, these shocks lead to upward pressure on long rates.

Additionally, given the large run up in debt over recent history, we calculate the long-run interest rate elasticity over a range of initial levels of debt and find it increases with the initial debt level. For example, if the economy has zero debt then a 1 percentage point increment in the debt to GDP ratio leads to a 1.5 bp increase in interest rates. Instead, if the debt equals GDP then the same increase in debt leads to a 1.8 bp increase in interest rates. The magnitude of the effects on interest rates increase with the level of debt because the strength of the savings channel declines with larger levels of pre-existing government debt because total households savings is already elevated in order to absorb the pre-existing debt.

Given that the size of the effects depend on the level of pre-existing debt and that the dynamic effects on long rates take many years to materialize and depend on the composition of the policy shocks, next we assess the effect on the current and future path of the interest rate from the large run up in government debt over the last

twenty five years. Leveraging the estimates of the composition of changes from the [Committee for Responsible Federal Budget \(2024\)](#), we trace out the dynamic effects on the interest rates from the change in public debt relative to the Congressional Budget Office projection path as of 2000. We find that the approximately 100 percentage points of additional debt as of 2023, relative to CBO's expected path as of 2000, leads to a total of 180 bp upward pressure on the 10 year interest rate. However, even if we assume that no additional debt will be accumulated after 2023, we find that due to the slow moving dynamics of the effects from the particular composition of policies underlying this accumulated debt, only 100 bp of the eventual interest rate increase has been realized to date. Thus, there is still significant upward pressure on interest rates from the current level of debt to come over the next several decades.

Finally, we revisit the empirical estimation strategy to understand how previous attempts to summarize the dynamics between debt and interest rates with one elasticity relate to our findings. First, we build on the empirical strategy employed by the past literature, but we introduce several methodological updates. First, the past literature, notably in [Engen and Hubbard \(2004\)](#) and [Laubach \(2009\)](#), confronts endogeneity concerns from business cycle shocks that may occur at the same time as changes in public debt (e.g., due to countercyclical fiscal policy) by focusing on the relationship between the *expected levels* of interest rates and public debt as a share of GDP. Specifically, they consider long term expectations using CBO's projections for future debt and the forward rate (i.e. the projection of future interest rates based off the yield curve). By considering these long term expectations, the authors identify the relationship after the component of short term business cycle shock has presumably died out. However, estimating the relationship in levels creates a potential for bias due to non-stationarity in public debt-to-GDP ratios, and thus we alleviate this concern by estimating the relationship in first differences. Additionally, we use newer public debt projections from the CBO that extend the forecast horizon at which we estimate public debt and interest rates (from 5 years in prior work to 10 years in this paper).⁵ The ten year projections are more consistent with the overall effect on long run U.S. debt, particularly because deficit financed fiscal policies tend to be in effect past five years. With our updated methodology and data, we find that estimated elasticities of 1 to 1.5 basis points, which are in line with our quantitative results, but

⁵In addition, reformulating the empirical specification in first differences additionally allows us to decompose overall public debt into changes due to the primary debt and due to net interest payments. We focus only on the primary debt since net interest payments introduce a concern over reverse causality, that higher interest rates mechanically increase government debt by increasing government borrowing costs. Finally, we include additional controls to capture potential correlation with the business cycle and population growth.

these estimates are considerably smaller than most previous estimates of 2 to 5 basis points, primarily due to introducing longer forecast horizons.

Importantly this estimation strategy provides insight into the average response of interest rates with respect to the level and historical changes in public debt. However, as we demonstrate quantitatively, there can be considerable variation in these elasticities depending on the term of the interest rate, the level of debt, and the type of fiscal policy shock generating the debt. Although given the limited data we are not able to separately estimate the elasticity for different levels of debt, we are able to estimate separate elasticities from different sources of changes in debt (tax revenues, mandatory outlays and discretionary outlays) and over different horizons. Although we are unable to statistically confirm the heterogeneity in part due to limited power from the data, we find considerable differences in point estimates across sources, ranging from -8 to 1.8 basis points. Moreover, we find that the estimates are sensitive to both how far in the future the forward rate is measured along with the length of the maturity. Thus, taken as a whole both the quantitative and empirical results indicate that it is incorrect to consider one homogeneous interest rate elasticity for long term interest rates with respect to debt and instead one must differentiate across types of debt financed policies along with the terms of the interest rate even at the longer end of the yield curve and instead one must consider the full dynamic path of how interest rates respond to the particular public debt.

Related Literature. This paper is related to several strands of research on the relationship between interest rates and changes to the macroeconomy, with a focus on policy implications.

This paper builds on seminal estimates of the interest rate elasticity with respect to changes in public debt, such as [Engen and Hubbard \(2004\)](#), [Gale and Orszag \(2004\)](#), and [Laubach \(2009\)](#). These papers devise strategies for isolating the effects of fiscal policy from other macroeconomic shocks that may cause the interest rate to vary, such as business cycle shocks. Their general approach was to regress the level of N -year ahead interest rates on the level of forecasted N -year ahead public debt, after controlling for a host of macroeconomic conditions relevant to interest rate determination, so that short-term shocks and fluctuations have little or no impact on the fiscal measures. [Gamber and Seliski \(2019\)](#) and [Neveu and Schafer \(2024\)](#) replicate the methodology from these seminal papers using more recent data and find evidence of a structural break after in estimates after the Great Recession. Relative to these papers, we make several methodological improvements that address estimation bias from non-stationarity in the evolution of public debt, and endogeneity in the public debt measure which includes a short-term interest rate component from

the payment of preexisting debt obligations and can therefore the interest rate may respond macroeconomic shocks that are unrelated to the evolution of public debt.⁶ Concurrently with this work, [Plante et al. \(2025\)](#) have also found that eliminating bias from non-stationarity leads to lower estimates for the interest rate elasticity.

This interest rate elasticity can be an important consideration in a recent strand of literature examining debt sustainability when real interest rates are lower than the economy's growth rate, as they have been in the U.S. over recent history. For example, [Blanchard \(2019, 2022\)](#) demonstrates that under these circumstances the level of debt can eventually stabilize even if the government runs a persistent primary deficit.⁷ However, as [Blanchard \(2022\)](#) points out, with a sufficiently large interest rate elasticity, an increase in debt may cause borrowing rates to exceed economic growth rates. [Mian et al. \(2025\)](#) provide a formal condition to incorporate this elasticity, in particular when the difference between the interest and growth rates lie below the interest rate elasticity of the debt.⁸ Related, [Angeletos et al. \(2023\)](#) show that with incomplete markets (e.g. that violate Ricardian Equivalence) fiscal deficits can partially finance themselves by generating increased activity that enlarges the tax base and lowers real debt through inflation. Our paper demonstrates that when examining the implications of the dynamic interest rate response for debt sustainability it is important to consider the composition of policies generating the debt.

Finally, this paper provides a countervailing force to a literature on the causes of the recent fall in – or “secular stagnation” of – natural interest rates such as population aging ([Eggertsson et al. \(2019\)](#)), the global saving glut ([Bernanke \(2005\)](#)) a shortage of safe assets ([Caballero et al. \(2017\)](#)) and income inequality ([Auclert and Rognlie \(2020\)](#)).⁹ Most closely related is [Rachel and Summers \(2019\)](#) and [Platzer and Peruffo](#)

⁶[Barro \(1979\)](#) shows that even when Ricardian equivalence holds, public debt may increase the efficiency of the economy by smoothing distortionary tax rates over time, and that the public debt-to-GDP ratio is not mean reverting over time. In contrast, using data from 1916-1995, [Bohn \(1998\)](#) shows that the primary surplus increases with the debt-to-GDP ratio, and that the debt-to-GDP ratio is indeed stationary. [Campbell et al. \(2023\)](#) have recently updated these results and find that neither the primary surplus-to-GDP nor the public debt-to-GDP ratios are stationary, while the tax revenues are indeed stationary.

⁷Other recent papers have focused more on other types of debt sustainability. A prominent example is [Fourakis and Karabarbounis \(2024\)](#) that looks at the relationship between public debt and interest rate *spreads* after a large macroeconomic shock, the onset of COVID in this case.

⁸Similarly, [Aguiar et al. \(2024\)](#) find that a similar condition holds in a standard incomplete market model when a policy can redistribute resources in a Pareto efficient way.

⁹For estimates of this rate see [Del Negro et al. \(2017\)](#), [Holston et al. \(2017\)](#), [Johannsen and Mertens \(2018\)](#), [Kiley \(2020\)](#), [Lubik and Matthes \(2015\)](#), [Gomme et al. \(2011\)](#). Similarly, long rates were relatively low over this period. Relatedly, rates on public bonds have fallen over this period (see [Reis \(2022\)](#)). See [Bauer and Rudebusch \(2016\)](#), [Levrero and Deleidi \(2019\)](#), and [Reis \(2025\)](#) for useful discussion around these points.

(2022), which use structural models to measure the relative strengths of these various factors that account for the downward trend in the natural interest rate, as well as the upward pressure on trend interest rates from increased public debt. Our results map out the dynamic interest rate response of the debt accumulated over the last twenty five years which point to continued notable upward pressure on the interest rate going forward even without anymore debt being accumulated.

Importantly, the difference across policies in the dynamic interest rate response in our paper is due to variation in the strength of the saving channel across policies and over time. In this vein, [Kaplan \(2025\)](#) considers how fiscal policy distributes resources across households and how the timing of those policies is central to how long lasting their effect is.¹⁰ Moreover, several recent papers have considered how distributional effects can interact with the savings channel. [Peterman and Sager \(2022\)](#) calibrate a quantitative life cycle model with incomplete markets to match wealth and income distributions by age, and find that public debt lowers welfare by increasing the variation in consumption over the life cycle and exacerbating wealth inequality. [Mian et al. \(2020\)](#) document that wealthy households generate a large stockpile of savings when top income shares increase, as these households have a higher propensity to save out of lifetime income, while [Mian et al. \(2021\)](#) develop a model in which households at the top of the wealth distribution eventually exert such a strong effect on the aggregate interest rate that households at the bottom of the wealth distribution begin to borrow at a higher rate and aggregate demand decreases. Finally, [Fagereng et al. \(2019\)](#) show in Norwegian data that saving rates increase with wealth when including capital gains in wealth measures, because wealthy households enjoy a flow of income from these assets.

Outline. The remainder of this paper is organized as follows. [Section 2](#) details our model and characterizes the economic environment. [Section 3](#) details our calibration strategy and the model’s quantitative fit to the data. [Section 4](#) considers policy counterfactuals that characterize the relationship between government debt and interest rates. Finally, [Section 5](#) updates the canonical empirical estimates of this relationship and compares them to our model results. [Section 6](#) concludes.

¹⁰Importantly, we employ global solution methods in our computations. [Bianchi and Kaplan \(2026\)](#) demonstrate that local solution methods such as linearization are not accurate when tracing out the economic response from fiscal policies as large as those leading to the run up in the debt over the last few decades.

2 Economic Environment

We consider the economic effects of a change in public debt within a quantitative life cycle model with incomplete markets. The model is adapted from [Peterman and Sager \(2022\)](#) and extended to include foreign capital inflows. We define the stationary recursive competitive equilibrium around a balanced growth path. For ease of explication, we present the detrended stationary recursive competitive equilibrium and suppress time-dependence in our notation. However, we make explicit any primitives that require additional assumptions for the model to be consistent with balanced growth.

2.1 Production

We assume there exists a large number of firms that sell a single consumption good in a perfectly competitive product market, purchase inputs from perfectly competitive factor markets, and each operate an identical constant returns to scale production technology, $Y = ZF(K, L)$. These assumptions on primitives admit a representative firm that chooses capital (K) and labor (L) inputs in order to maximize profits, given an interest rate r , a wage rate w , a level of total factor productivity Z , and capital depreciation rate $\delta \in (0, 1)$. Following [Aiyagari and McGrattan \(1998\)](#), we assume that total factor productivity grows over time at rate $g_z > 0$ which generates output growth at rate denoted by $g_y > 0$.

2.2 Households

Demographics: Time is discrete and each model period represents a year. The household is the unit of measurement within our model and each period the economy is inhabited by J overlapping generations of households. Each period a new cohort is born and the size of each successive newly born cohort grows at a constant rate $g_n > 0$. All households live for a maximum of J periods, where age is indexed by $j = 1, \dots, J$. All living households face mortality risk such that, conditional on living to age j , ψ_j is the probability of an age- j household living to age $j + 1$. Accordingly, the terminal-age survival probability is $\psi_J = 0$.

Preferences: Households derive utility from lifetime paths of consumption, labor hours, retirement status and assets, denoted $\{c_j, h_j, d_j, a_{j+1}\}_{j=1}^J$, according to the fol-

lowing preferences:

$$\mathbb{E}_1 \sum_{j=1}^J \beta^{j-1} \left(\prod_{i=1}^{j-1} \psi_i \right) \left[u_j(c_j) - v(h_j, d_j) + \beta(1 - \psi_j) \phi(a_{j+1}) \right]$$

where β is the time discount factor, $u_j(c)$ and $v(h, d)$ are instantaneous utility functions over consumption, labor hours and retirement status, respectively, satisfying standard conditions.¹¹ Households derive instantaneous utility $\phi(a_{j+1})$ from bequeathing their assets, should they receive a mortality shock and die. Expectations are taken with respect to the stochastic processes governing labor productivity.

Between the ages J_{ret} and $\bar{J}_{ret}$, a household makes the irreversible decision whether to retire, and once retired an agent no longer has the option to work. Any household that has not retired by age $\bar{J}_{ret}$ is forced to retire. We denote the age at which a household chooses to retire by J_{ret} and define $d_j \equiv \mathbb{1}(j < J_{ret})$ to be an indicator variable that equals one when a household chooses to continue working and zero upon retirement.

Labor Earnings: Non-retired households are endowed with one unit of time per period, which they split between leisure and market labor. During each period of working life, an household's labor earnings are $we_j h_j$, where w is the wage rate per efficiency unit of labor, e_j is the household's idiosyncratic labor productivity drawn at age j , and h_j is the share of the time endowment that the household chooses to work at age j .

Following [Kaplan \(2012\)](#), we assume that labor productivity shocks can be decomposed into four sources:

$$\log(e_j) = \kappa + \theta_j + v_j + \epsilon_j$$

where (i) $\kappa \stackrel{iid}{\sim} \mathcal{N}(0, \sigma_\kappa^2)$ is an individual-specific fixed effect that is drawn once when the household enters the economy and remains fixed, (ii) $\{\theta_j\}_{j=1}^J$ is an age-specific fixed effect that evolves over the life cycle in a predetermined manner, (iii) v_j is a persistent shock that follows a first-order Markov process, and (iv) $\epsilon_j \stackrel{iid}{\sim} \mathcal{N}(0, \sigma_\epsilon^2)$ is a transitory shock that is drawn each period.

For notational compactness, we denote the relevant state as a vector $\varepsilon_j = (\kappa, \theta_j, v_j, \epsilon_j)$ that contains each element necessary for computing contemporaneous labor earn-

¹¹The instantaneous utility over consumption accounts for changes in household size through an adult equivalent normalization and therefore varies with age, which we detail in [Section 3](#). Furthermore, this definition of preferences embeds the assumption that the disutility of labor, $v(h, d)$, and utility from bequests, $\phi(a)$, grow over time. In particular, along a balanced growth path they will grow at the same rate as the utility over individual consumption (for more detail see [Appendix B](#)).

ings, $e_j \equiv e(\varepsilon_j)$, and forming expectations about future labor earnings. Denote the Markov process governing the process for ε by $\pi_j(\varepsilon_{j+1}|\varepsilon_j)$ for each ε_j , ε_{j+1} and for each $j = 1, \dots, \bar{J}_{ret}$.

Assets and Bequests: Households have access to a single asset, a non-contingent one-period bond denoted a_j with a market determined rate of return of r . Households are endowed with zero initial wealth, such that $a_1 = 0$ for each household. Working households may take on a net debt position, in which case they are subject to a borrowing constraint that requires their net assets be bounded below by $\underline{a} \in \mathbb{R}$ and face an interest rate on repayment of r/ψ_j at each age.¹² For notational convenience we define $\tilde{r}_j(a)$ as the interest rate that takes on a value of r when $a \geq 0$ and r/ψ_j when $\underline{a} \leq a < 0$.

If households hold assets when they die those assets are redistributed to living households as bequests. During their lifetimes, households receive a flow of bequests at each age (including upon entering the economy). This flow of bequests varies with the individual-specific fixed effect component of labor productivity and age according to the function $b_j(\kappa)$.

Medical Expenditures: Given the potential for households' late-life expenses to affect lifetime savings decisions, we incorporate out-of-pocket medical expenditures into the model. Households face medical expenses that deterministically as a function of age, denoted μ_j , beginning at age 70 and face zero medical expenses prior to age 70. We focus on late-life medical expenditures because previous work, notably [DeNardi, French, and Jones \(2010\)](#), finds that average out-of-pocket expenditures rise rapidly after age 70 and begin to constitute a notable share of household expenditures.¹³

2.3 Government

The government (i) consumes resources G , (ii) collects Social Security taxes and distributes Social Security payments to retired households, (iii) distributes bequests across living households, (iv) distributes transfers to cover a portion of medical expenses and (v) collects income taxes from each household.

Social Security: The model's Social Security Program is financed with a payroll tax,

¹²While the baseline model assumes that households can freely adjust their savings when unconstrained, we consider how sensitive our results are to adding frictions to households' ability to dissave in [Section 4.5](#).

¹³For example, [DeNardi et al. \(2016\)](#) find that average out-of-pocket medical expenditures rise from \$1000 at age 75 to \$17,700 by age 100.

τ_{ss} , and taxable income is capped per-period by $\bar{m}$. Therefore, the consumer pays a payroll tax given by: $\tau_{ss} \min\{weh, \bar{m}\}$.

Social security payments are computed using the averaged indexed monthly earnings (AIME) that summarizes a household's lifetime labor earnings. Following [Huggett and Parra \(2010\)](#) and [Kitao \(2014\)](#), the AIME is denoted by $\{m_j\}_{j=1}^J$, has an initial value $m_1 = 0$ and evolves as follows:

$$m_{j+1} = \begin{cases} \frac{1}{j} (\min\{we_j h_j, \bar{m}\} + (j-1)m_j) & \text{for } j \leq 35 \\ \max \left\{ m_j, \frac{1}{j} (\min\{we_j h_j, \bar{m}\} + (j-1)m_j) \right\} & \text{for } j \in (35, J_{ret}) \\ m_j & \text{for } j \geq J_{ret} \end{cases}$$

The AIME is a state variable for determining future benefits. Benefits are derived from the AIME in two steps: a base payment is determined, and then the base payment is adjusted according to a household's retirement age. The base payment, denoted by $b_{base}^{ss}(m_{J_{ret}})$, is computed as a piecewise-linear function over the household's average labor earnings at retirement $m_{J_{ret}}$:

$$b_{base}^{ss}(m_{J_{ret}}) = \begin{cases} \tau_{r1} m_{J_{ret}} & \text{for } m_{J_{ret}} \in [0, b_1^{ss}) \\ \tau_{r1} b_1^{ss} + \tau_{r2} (m_{J_{ret}} - b_1^{ss}) & \text{for } m_{J_{ret}} \in [b_1^{ss}, b_2^{ss}) \\ \tau_{r1} b_1^{ss} + \tau_{r2} b_2^{ss} + \tau_{r3} (m_{J_{ret}} - b_1^{ss} - b_2^{ss}) & \text{for } m_{J_{ret}} \in [b_2^{ss}, b_3^{ss}) \\ \tau_{r1} b_1^{ss} + \tau_{r2} b_2^{ss} + \tau_{r3} b_3^{ss} & \text{for } m_{J_{ret}} \geq b_3^{ss} \end{cases}$$

The base payment is adjusted according to a household's retirement age to penalize early retirement and credit delayed retirement. The adjustment is given by:

$$b_{ss}(m_{J_{ret}}) = \begin{cases} (1 - D_1(J_{nra} - J_{ret})) b_{base}^{ss}(m_{J_{ret}}) & \text{for } \underline{J}_{ret} \leq J_{ret} < J_{nra} \\ (1 + D_2(J_{ret} - J_{nra})) b_{base}^{ss}(m_{J_{ret}}) & \text{for } J_{nra} \leq J_{ret} \leq \bar{J}_{ret} \end{cases}$$

where $D_i(\cdot)$ are functions governing the benefits penalty or credit, and J_{nra} is the "normal retirement age".

Income Taxation: Taxable income is defined as the sum of labor income and capital income from assets and bequests, net of social security contributions from an employer

which are considered half of the total contribution:

$$y_j(h, a, \varepsilon, d) \equiv \begin{cases} we(\varepsilon)h + \tilde{r}_j(a)a + rb_j(\varepsilon) - \frac{\tau_{ss}}{2} \min\{we(\varepsilon)h, \bar{m}\} & \text{if } d = 1 \\ r(a + b_j(\varepsilon)) & \text{if } d = 0 \end{cases}$$

The government taxes each household's taxable income according to an increasing and concave function, $Y(y_j(h, a, e, d))$.

Medical Transfers: In the spirit of U.S. Medicaid program and other means-tested public assistance programs, low-income households are given transfers in order to allow them to pay for medical expenses and still have resources available for consumption. The government provides transfers to retired households after the age $\bar{j}_{ret}$ that guarantee a minimum consumption level, denoted $\underline{c} > 0$, after paying medical expenditures and taxes. The transfers are given by,

$$Tr_j(a, m, \varepsilon) = \max \left\{ 0, \underline{c} - [b_{ss}(m) + r(a + b_j(\varepsilon)) - Y(r(a + b_j(\varepsilon))) - \mu_j] \right\}$$

where households do not receive a transfer if their after-tax income net of medical expenses allows for consumption in excess of the policy's minimum guarantee ($\underline{c}$).¹⁴

Public Savings and Budget Balance: Each period, the government has a debt balance B and saves or borrows (denoted B') at the market interest rate r . If the government borrows, then $B' < 0$ and the government repays rB' next period. If the government saves, then $B' > 0$ and the government collects asset income rB' next period. The resulting government budget constraint is:

$$G + Tr + (1 + g_y)B' - B = rB + R \quad (1)$$

where R is aggregate revenues from income taxation and G is the level of government expenditures that are independent from aggregate medical transfers, Tr .¹⁵ The model's Social Security system is self-financing and therefore does not appear in the

¹⁴We only model these transfers for non-working households because the consumption floor is sufficiently low to be effectively irrelevant for working households. Working households only need to spend a small fraction of their time endowment to generate enough income to relax the consumption floor and, thus, there would be no medical related transfers to working households even if explicitly allowed.

¹⁵We assume government expenditures exclusive of aggregate medical transfers, G , are unproductive. Two recent papers, [Röhrs and Winter \(2017\)](#) and [Chatterjee, Gibson, and Rioja \(2017\)](#) have relaxed the standard Ramsey assumption that government expenditures are unproductive. Both papers show that public savings is optimal with productive government expenditures, intuitively because there is an additional benefit to aggregate output.

governmental budget constraint.

2.4 Consumer's Problem

The household's state is $(a, \varepsilon, m, d_{-1})$ and consists of asset holdings a , labor productivity shocks $\varepsilon \equiv (\kappa, \theta, \nu, \epsilon)$, Social Security contribution (AIME) variable m , and retirement status d_{-1} .

Prior to retirement age, the age- j household's recursive problem is:

$$V_j(a, \varepsilon, m, 1) = \max_{c, a', h} [u_j(c) - v(h, 1)] + [\beta(1 + g_w)^{1-\sigma}] \psi_j \sum_{\varepsilon'} \pi_j(\varepsilon' | \varepsilon) V_{j+1}(a', \varepsilon', m', 1) + [\beta(1 + g_w)^{1-\sigma}] (1 - \psi_j) \phi(a') \quad (2)$$

subject to

$$\begin{aligned} c + (1 + g_w)a' &\leq we(\varepsilon)h + (1 + \tilde{r}_j(a))a + (1 + r)b_j(\varepsilon) - \tau_{ss} \min\{we(\varepsilon)h, \bar{m}\} - Y(y_j(h, a, \varepsilon, 1)) \\ a' &\geq \underline{a} \end{aligned}$$

where g_w is the steady state rate of wage growth and σ is the coefficient of relative risk aversion (see [Section 3](#) for the underlying utility specification).

A working household chooses whether to retire (indicated by $d = 0$) or not ($d = 1$) between ages $\underline{J}_{ret}$ and $\bar{J}_{ret}$ or faces mandatory retirement after age $\bar{J}_{ret}$. The retired age- j household's stationary recursive problem is:

$$V_j(a, \varepsilon, m, 0) = \max_{c, a'} u_j(c) + [\beta(1 + g_w)^{1-\sigma}] \psi_j V_{j+1}(a', \varepsilon, m, 0) + [\beta(1 + g_w)^{1-\sigma}] (1 - \psi_j) \phi(a') \quad (3)$$

subject to

$$\begin{aligned} c + (1 + g_w)a' &\leq (1 + r)(a + b_j(\varepsilon)) + b_{ss}(m) - Y(r(a + b_j(\varepsilon))) + (Tr_j(a, m, \varepsilon) - \mu_j) \\ a' &\geq \underline{a} \end{aligned}$$

where the post-retirement state ε simply records productivity type κ for determining bequest inflows. The construction of the stationary Bellman equation is presented in [Appendix B](#).

2.5 Foreign Sector

Since foreign investment in U.S. assets affects the level of productive capital and therefore the interest rate, we assume that foreigners can invest in the domestic market. The foreign sector is characterized by a representative investor that purchases claims on domestic government debt and domestic private capital, the stock of which is denoted F . In our baseline model, we assume that the level of foreign holdings (F) is exogenously determined.

2.6 Stationary Recursive Competitive Equilibrium

We study a stationary equilibrium along a balanced growth path in which all aggregate variables grow at the same rate as output, g_y .

Households are heterogeneous with respect to their age $j \in \mathbf{J} \equiv \{1, \dots, J\}$, wealth $a \in \mathbf{A}$, labor productivity $\varepsilon \in \mathbf{E}$, average lifetime earnings $m \in \mathbf{X}$, and retirement status $d \in \mathbf{D} \equiv \{0, 1\}$. Let $\mathbf{S} \equiv \mathbf{A} \times \mathbf{E} \times \mathbf{X} \times \mathbf{D}$ be the state space and $\mathcal{B}(\mathbf{S})$ be the Borel σ -algebra on $\mathbf{S}$. Let $\mathbf{M}$ be the set of probability measures on $(\mathbf{S}, \mathcal{B}(\mathbf{S}))$. Then $(\mathbf{S}, \mathcal{B}(\mathbf{S}), \lambda_j)$ is a probability space in which $\lambda_j(S) \in \mathbf{M}$ is a probability measure defined on subsets of the state space, $S \in \mathcal{B}(\mathbf{S})$, that describes the distribution of individual states across age- j households. Denote the fraction of the population that is age $j \in \mathbf{J}$ by ω_j . For each set $S \in \mathcal{B}(\mathbf{S})$, $\omega_j \lambda_j(S)$ is the fraction of age $j \in \mathbf{J}$ and type $S \in \mathbf{S}$ households in the economy. We can now define a stationary recursive competitive equilibrium of the economy.

Definition (Equilibrium): Given a government policy (B', B, G, Y) and level of foreign investment, a *stationary recursive competitive equilibrium* is (i) an allocation for consumers described by policy functions $\{c_j, a'_j, h_j, d_j\}_{j=1}^J$ and consumer value function $\{V_j\}_{j=1}^J$, (ii) an allocation for the representative firm (K, L) , (iii) prices (w, r) , (iv) bequests $b_j(\kappa)$, (v) a government policy $(\tau_{ss}, b_{ss}, \underline{c})$, and (vi) distributions over households' state vector at each age $\{\lambda_j\}_{j=1}^J$ that satisfy:

- (a) Given prices, policies and bequests, $V_j(a, \varepsilon, m, d_{-1})$ solves the Bellman equation (2) and (3) with associated policy functions $c_j(a, \varepsilon, m, d_{-1})$, $a'_j(a, \varepsilon, m, d_{-1})$, $h_j(a, \varepsilon, m, d_{-1})$ and $d_j(a, \varepsilon, m, d_{-1})$.
- (b) Given prices (w, r) , the representative firm's allocation minimizes cost, $r = ZF_K(K, L) - \delta$ and $w = ZF_L(K, L)$.
- (c) Total bequests from households of type- κ who die at the end of this period are distributed across next period's living households of type- κ according to the function

$b_j(\kappa)$. Then the following condition must hold for each κ ,

$$(1 + g_n)\pi(\kappa) \sum_{j=1}^J \omega_j b_j(\kappa) = \sum_{j=1}^J \omega_j (1 - \psi_j) \int a'_j(a, \varepsilon, m, d_{-1} | \kappa) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1} | \kappa),$$

such that living households' savings equal next period's wealth net of bequests,

$$\sum_{j=1}^J \omega_j \psi_j \int a'_j(a, \varepsilon, m, d_{-1} | \kappa) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1} | \kappa) = (1 + g_n) \sum_{j=1}^J \omega_j \int a \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1} | \kappa)$$

where $\lambda(a, \varepsilon, m, d_{-1} | \kappa)$ denotes the mass over $(a, \varepsilon, m, d_{-1})$ when holding the value of κ fixed, such that $\pi(\kappa) = \int \mathbf{d}\lambda(a, \varepsilon, m, d_{-1} | \kappa)$ is the measure of type- κ households.

- (d) Government policies satisfy budget balance in [Equation \(1\)](#), where aggregate income tax revenue is given by:

$$R \equiv \sum_{j=1}^J \omega_j \int Y(y_j(h_j(a, \varepsilon, m, d_{-1}), a, \varepsilon, d_j(a, \varepsilon, m, d_{-1}))) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}), \quad (4)$$

and aggregate medical expenditure transfers are given by:

$$Tr \equiv \sum_{j=\bar{j}_{ret}+1}^J \omega_j \int Tr_j(a, m, \varepsilon; \underline{c}) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}).$$

- (e) Social security is self-financing:

$$\begin{aligned} & \sum_{j=1}^J \omega_j \int d_j(a, \varepsilon, m, d_{-1}) \tau_{ss} \min\{we(\varepsilon)h_j(a, \varepsilon, m, d_{-1}), \bar{m}\} \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}) \\ &= \sum_{j=1}^J \omega_j \int (1 - d_j(a, \varepsilon, m, d_{-1})) b_{ss}(m) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}). \end{aligned} \quad (5)$$

- (f) Given policies and allocations, prices clear asset and labor markets:

$$K - B = \sum_{j=1}^J \omega_j \int (a + b_j(\kappa)) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}) + F \quad (6)$$

$$L = \sum_{j=1}^J \omega_j \int d_j(a, \varepsilon, m, d_{-1}) e(\varepsilon) h_j(a, \varepsilon, m, d_{-1}) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}) \quad (7)$$

and the allocation satisfies the resource constraint (guaranteed by Walras' Law):

$$C + (1 + g_y)K' + G + Tr = ZF(K, L) + (1 - \delta)K \quad (8)$$

where

$$C = \sum_{j=1}^J \omega_j \int c_j(a, \varepsilon, m, d_{-1}) \mathbf{d}\lambda_j(a, \varepsilon, m, d_{-1}).$$

- (g) Given consumer policy functions, distributions across age j households $\{\lambda_j\}_{j=1}^J$ are given recursively from the law of motion $T_j^* : \mathbf{M} \rightarrow \mathbf{M}$ for all $j \in \mathbf{J}$ such that T_j^* is given by:

$$\lambda_{j+1}(\mathcal{A} \times \mathcal{E} \times \mathcal{X} \times \mathcal{D}) = \sum_{d_{-1} \in \{0,1\}} \int_{\mathcal{A} \times \mathcal{E} \times \mathcal{X}} Q_j((a, \varepsilon, m, d_{-1}), \mathcal{A} \times \mathcal{E} \times \mathcal{X} \times \mathcal{D}) \mathbf{d}\lambda_j$$

where $\mathcal{S} \equiv \mathcal{A} \times \mathcal{E} \times \mathcal{X} \times \mathcal{D} \subset \mathbf{S}$, and $Q_j : \mathbf{S} \times \mathcal{B}(\mathbf{S}) \rightarrow [0, 1]$ is a transition function on $(\mathbf{S}, \mathcal{B}(\mathbf{S}))$ that gives the probability that an age- j household with current state $\mathbf{s} \equiv (a, \varepsilon, m, d_{-1})$ transits to the set $\mathcal{S} \subset \mathbf{S}$ at age $j + 1$. The transition function is given by:

$$Q_j((a, \varepsilon, m, d_{-1}), \mathcal{S}) = \begin{cases} \psi_j \cdot \pi_j(\mathcal{E}|\varepsilon)^{d_{-1}} & \text{if } a'_j(\mathbf{s}) \in \mathcal{A}, m'_j(\mathbf{s}) \in \mathcal{X}, d_j(\mathbf{s}) \in \mathcal{D} \\ 0 & \text{otherwise} \end{cases}$$

where households that continue working and transition to set $\mathcal{E}$ choose $d_j(\mathbf{s}) = 1$, while households that transition from working life to retirement choose $d_j(\mathbf{s}) = 0$. For $j = 1$, the distribution λ_j reflects the invariant distribution $\pi_{ss}(\varepsilon)$ of initial labor productivity over $\varepsilon = (\kappa, \theta_1, 0, \epsilon_1)$.

- (h) Aggregate capital, governmental debt, prices and the distribution over consumers are stationary, such that $K' = K$, $B' = B$, $w' = w$, $r' = r$, and $\lambda'_j = \lambda_j$ for all $j \in \mathbf{J}$.

3 Calibration

3.1 Parameters and Functional Specifications

In this section we calibrate the life cycle model along the balanced growth path, drawing largely from the calibration in [Peterman and Sager \(2022\)](#). There are two subsets of parameters. One subset is set directly from empirical estimates, while the other subset is chosen so that the model matches a number of empirical moments. [Table 1](#) summarizes the target, source and value for each parameter, and [Table 2](#) evaluates model fit by comparing model generated moments to empirical moments.

Production: We assume that the aggregate production function is Cobb-Douglas of the form $F(K, L) = K^\alpha L^{1-\alpha}$ where $\alpha = 0.36$ is the income share accruing to capital and total factor productivity is normalized to one, $Z = 1$. The depreciation rate is set to $\delta = 0.1$ which allows the model to match the empirically observed investment-to-output ratio of 26%.¹⁶

Demographics: Households enter the economy at age 20 (or model age $j = 1$) and we set conditional survival probabilities $\{\psi_j\}_{j=1}^{J-1}$ to match survival rates for households in the data from [Bell and Miller \(2002\)](#). We impose that surviving households exogenously die after age 100 (or model age $J = 81$) by setting the terminal survival probability $\psi_J = 0$. Household mortality is defined as either both members of a married household dying or the sole remaining adult of a household dying. Household mortality rates account for demographic changes within the household and variation in individuals' mortality rates by age and sex. We set the population growth rate to $g_n = 0.011$ to match annual population growth in the US.

Preferences: The utility function is separable in the utility over consumption, $u_j(c)$, labor hours and retirement, $v(h, d)$, and bequests, $\phi(a')$. We parameterize the utility specification as,

$$u_j(c) = \frac{(c/n_j)^{1-\sigma}}{1-\sigma}$$

$$v(h, d) = \chi_1 \frac{h^{1+\frac{1}{\gamma}}}{1+\frac{1}{\gamma}} + d\chi_2$$

$$\phi(a') = \chi_b \frac{(\chi_a + a')^{1-\sigma}}{1-\sigma}.$$

¹⁶We calculate the ratio as the average of private investment in fixed assets and consumer durables relative to GDP from 2001 to 2008.

Table 1: Calibration Targets and Parameters for Baseline Economy.

Description	Parameter	Value	Target or Source
Demographics			
Maximum Age	J	81 (100)	By Assumption
Min/Max Retirement Age	$\underline{J}_{ret}, \bar{J}_{ret}$	43, 51 (62, 70)	Social Security Program
Population Growth	g_n	1.1%	Conesa et al (2009)
Survival Rate	$\{\psi_j\}_{j=1}^J$		Bell and Miller (2002)
Preferences and Borrowing			
Coefficient of RRA	σ	2.0	Conesa et al (2009)
Frisch Elasticity	γ	0.5	Kaplan (2012)
Coefficient of Labor Disutility	χ_1	166.0	Avg. Hours Worked = 0.2687
Fixed Utility Cost of Labor	χ_2	2.87	70% retire by NRA
Discount Factor	β	0.999	Capital/Output = 2.6
Borrowing Limit	$\underline{a}$	-0.375	Avg. Borrowing/Avg. Wealth = -0.0483
Bequests			
Coefficient on Bequest Utility	χ_b	60.5	Avg. Bequest/ Avg. Wealth = 0.0088
Non-Homotheticity of Bequests	χ_a	6.3	Bequests, 90th pct/Avg. Labor Earnings = 10.7
Bequest Age-Profile	$\{b_j(\kappa)\}_{j=1}^J$		Feiveson and Sabelhaus (2019)
Production Technology			
Capital Share	α	0.36	NIPA
Capital Depreciation Rate	δ	0.1	Investment/Output = 0.26
Output Growth	g_y	1.85%	NIPA
Labor Productivity			
Persistent Shock, autocorrelation	ρ	0.960	PSID
Persistent Shock, variance	σ_v^2	0.014	PSID
Permanent Shock, variance	σ_κ^2	0.054	PSID
Transitory Shock, variance	σ_ϵ^2	0.086	PSID
Mean Earnings, Age Profile	$\{\theta\}_{j=1}^J$		PSID
High Labor Productivity Shock	v_{max}	8.8	Top 20% Wealth = 83.4%
High Labor Prod. Persistence	p_S	99.4%	Top 20% Labor Share = 63.5%
High Labor Prod. Probability	π_S	0.5%	
Government Budget			
Government Consumption	$(G + Tr)/Y$	0.155	NIPA Average 1998-2007
Government Savings	B/Y	-0.611	NIPA Average 1998-2007
Marginal Income Tax	τ_0	0.258	Gouveia and Strauss (1994)
Income Tax Progressivity	τ_1	0.786	Gouveia and Strauss (1994)
Income Tax Progressivity	τ_2	4.125	Balanced Budget
Medical Expenses			
Consumption Floor (% of wL)	$\underline{c}$	15%	Kopecky and Koreshkova (2014)
Average Household Expenses	$\{\mu_j\}_{j=\underline{J}_{ret}}^J$		HRS-AHEAD
Social Security			
Payroll Tax	τ_{ss}	0.151	Balanced Budget
SS Replacement Rates	$\{\tau_{ri}\}_{i=1}^3$	(0.9, 0.32, 0.15)	Social Security Program
SS Replacement Bend Points	$\{b_i^{ss}\}_{i=1}^3$	(0.21, 1.29, 2.42)	Social Security Program
SS Early Retirement Penalty	$\{D_i\}_{i=1}^2$	See Text	Social Security Program

Utility over consumption is age-dependent in order to capture how a changing average household size over the life cycle affects household consumption decisions. Accordingly, we use the adult equivalent scale, n_j , to adjust consumption in the utility function. Following [Hur \(2018\)](#), we compute the adult equivalent scale at each age (of the head of household) to convert households of varying sizes into a standardized measure,

$$n_j \equiv \left[\omega_j^{single} \cdot 1 \right] + \left[(1 - \omega_j^{single}) \cdot 1.5 \right] + (1/3)n_j^c$$

where ω_j^{single} is the fraction of single-adult households with an age- j head of household, and n_j^c is the average number of children in a household with an age- j head of household.

Utility over consumption is a CRRA specification with a coefficient of relative risk aversion $\sigma = 2$, which is consistent with [Conesa et al. \(2009\)](#) and [Aiyagari and McGrattan \(1998\)](#). Disutility over labor exhibits a constant intensive margin Frisch elasticity. We choose $\gamma = 0.5$ such that the Frisch elasticity consistent with the majority of the related literature as well as the estimates in [Kaplan \(2012\)](#).¹⁷

We calibrate the labor disutility parameter χ_1 so that the cross sectional average of hours is 0.2687 of the time endowment, which we find in the PSID.¹⁸ Finally, χ_2 is the fixed utility cost of not being retired, which generates an active extensive margin by introducing a non-convexity in the utility function. We choose χ_2 to match the empirical observation that seventy percent of the population has retired by age 66.

We employ a standard utility function over bequests (c.f., [DeNardi \(2004\)](#)), where χ_b is a coefficient that determines the level of utility over bequests, and χ_a is a non-homothetic term that measures the extent to which bequests are luxury goods. We choose χ_b to match the bequest-to-wealth ratio of 0.0088 (see [Gale and Scholz \(1994\)](#)), and choose χ_a to match the 90th percentile of the bequest distribution for households over the age of 70, normalized by average labor income, of 10.7.

We choose discount factor β to match the average capital-output ratio of 2.6.¹⁹

Bequests: The total level of bequests to households is determined by the total amount of wealth held by households who died in the previous period. Bequests are redistributed to households with the same individual-specific labor productivity type, κ .

¹⁷ Although [Peterman \(2016\)](#) finds that estimates of the Frisch elasticity tend to be larger for non-primary earners, the Frisch elasticity of 0.5 still falls within the range of these estimates. Moreover, we have found that changing the Frisch elasticity within this range did not materially change the main results herein.

¹⁸ To compute hours worked in the PSID, we normalize a households' annual hours worked (by 40 hours per week, 52 weeks per year) and number of potential earners.

¹⁹ This is calculated as the average ratio of private fixed assets and consumer durables relative to GDP from 2002 to 2008.

For each type, these bequests are allocated to living households to match shares of bequests received by age in the Survey of Consumer Finances, according to the function $b_j(\kappa)$.

Liquidity Constraints: We choose the lower bound on assets $\underline{a} \leq 0$ so that the model matches the level of net wealth conditional on borrowing, relative to the total level of private wealth. This ratio is -4.83% in the 2007 Survey of Consumer Finances for ages 20 to 60.

Labor Productivity Process: The parameters for the labor productivity process are from [Peterman and Sager \(2022\)](#) which are jointly estimated from the PSID at the household level using the procedure described in [Kaplan \(2012\)](#).

A well known problem with a log-normal income process is that it cannot generate the degree of wealth and labor income inequality we observe in the data. To match the wealth and labor income distributions, we follow [Castañeda, Díaz-Giménez, and Ríos-Rull \(2003\)](#) and [Kindermann and Krueger \(2020\)](#), by modeling the persistent component of the labor productivity process in two parts. First, we include a standard persistent component of labor productivity which follows a standard first-order autoregressive process given by $v_{j+1} = \rho v_j + \eta_{j+1}$ with $\eta \stackrel{iid}{\sim} \mathcal{N}(0, \sigma_v^2)$ and $\eta_1 = 0$, which we estimate using the PSID. Second, we include an extremely high labor productivity state. We refer to this additional high labor productivity state as a *superstar shock* and we set the probability of receiving the superstar shock to 0.5%, which implies that 20% of households that retire at the normal retirement age experienced being a superstar at some point during their working lifetime. We choose the value of the superstar shock (v_{max}) and probability of remaining a superstar (p_S) so that the top 20% of the population holds 83.4% of total wealth and the top 20% of the population receives 53.5% of total labor income (see [Krueger, Mitman, and Perri \(2016\)](#)).²⁰ The value of v_{max} is 8.8, which implies that a superstar earns approximately 9 times more than the average non-superstar, and the value of p_S is 0.994, which implies that the superstar state is extremely persistent.

Foreign Investment: We choose F to match the 1990s average federal debt held by foreigners and international investors of 10.6 percent of GDP from the NIPA.

Government Debt and Income Taxation: Similarly to [Aiyagari and McGrattan \(1998\)](#), we set government debt equal to 61.1 percent of output, corresponding to the average

²⁰We assume that no household enters the economy as a superstar. We also assume that upon exiting the superstar state, households transition to the median persistent labor productivity state. Finally, superstars are not subject to the transitory labor productivity shock.

during the 1990s in the NIPA. We set the sum of government consumption and aggregate medical transfers to 15.5 percent of output. This ratio corresponds to the average of government expenditures to GDP from 1998 through 2007.²¹

We model the income tax using a standard functional form from [Gouveia and Strauss \(1994\)](#),

$$Y(y) = \tau_0 \left(y - (y^{-\tau_1} + \tau_2)^{-\frac{1}{\tau_1}} \right).$$

We parameterize the function with the authors' estimates of $\tau_0 = 0.258$ and $\tau_1 = 0.768$, and calibrate τ_2 to ensure the government budget constraint is satisfied.

Medical Expenditures and Transfers: Following [DeNardi, French, and Jones \(2010\)](#) and [Kopecky and Koreshkova \(2014\)](#), the consumption floor $\underline{c}$ is a stylized representation of the US Medicaid program and other means-tested public assistance programs. We set $\underline{c}$ to 15 percent of average labor earnings for all households until the normal retirement age (of 66 years old), which is the midpoint of estimates in [Kopecky and Koreshkova \(2014\)](#).²² Finally, we construct the age-dependent medical expenditures, $\{\mu_j\}$, to match average household out-of-pocket medical expenditures in the HRS-AHEAD dataset while accounting for household composition and survivorship.

Social Security: Consistent with the minimum and maximum retirement ages in the U.S. Social Security system, we set the interval in which households can retire to the ages 62 and 70, and we set the normal retirement age to 66. The early retirement penalty and delayed retirement credits are set in accordance with the Social Security program. In particular, if households retire up to three years before the normal retirement age, then households' benefits are reduced by 6.7 percent for each year they retire early. If they choose to retire four or five years before the normal retirement age, then benefits are reduced by an additional 5 percent for these years. If households choose to delay retirement past normal retirement age, then their benefits are increased by 8 percent for each year they delay. The marginal replacement rates in the progressive Social Security payment schedule $(\tau_{r1}, \tau_{r2}, \tau_{r3})$ are also set at their actual respective values of 0.9, 0.32 and 0.15. Following [Huggett and Parra \(2010\)](#), the bend points where the marginal replacement rates change $(b_1^{ss}, b_2^{ss}, b_3^{ss})$ and the maximum earnings $(\bar{m})$ are set equal to the actual multiples of mean earnings used in the U.S.

²¹We exclude government expenditures on Social Security since they are explicitly included in our model.

²²Using a different target (a 14% takeup rate in public transfers of this type), [Kopecky and Koreshkova \(2014\)](#) calibrate a very similar consumption floor of 16.5% of labor earnings. However, measuring the consumption floor is generally difficult, in part, because of the heterogeneity in programs available for different households.

Table 2: Target Moments, Model and Data

Moments	Data	Model
Capital-to-Output Ratio	2.595	2.597
Retired by age 66 (%)	0.700	0.700
Hours Worked up to age 66	0.269	0.269
Bequests-to-Wealth Ratio	0.009	0.010
Bequests, 90th pct / Avg. Labor Earnings	10.695	10.614
Top 20% Wealth Share	0.834	0.834
Top 20% Labor Income Share	0.635	0.638
Borrowers' Debt-to-Wealth	-0.048	-0.048

Social Security system so that b_1^{ss} , b_2^{ss} and $b_3^{ss} = \bar{m}$ occur at 0.21, 1.29 and 2.42 times average earnings in the economy. We set the payroll tax rate, τ_{ss} such that the program's budget is balanced. In our baseline model the payroll tax rate is 15.1 percent.

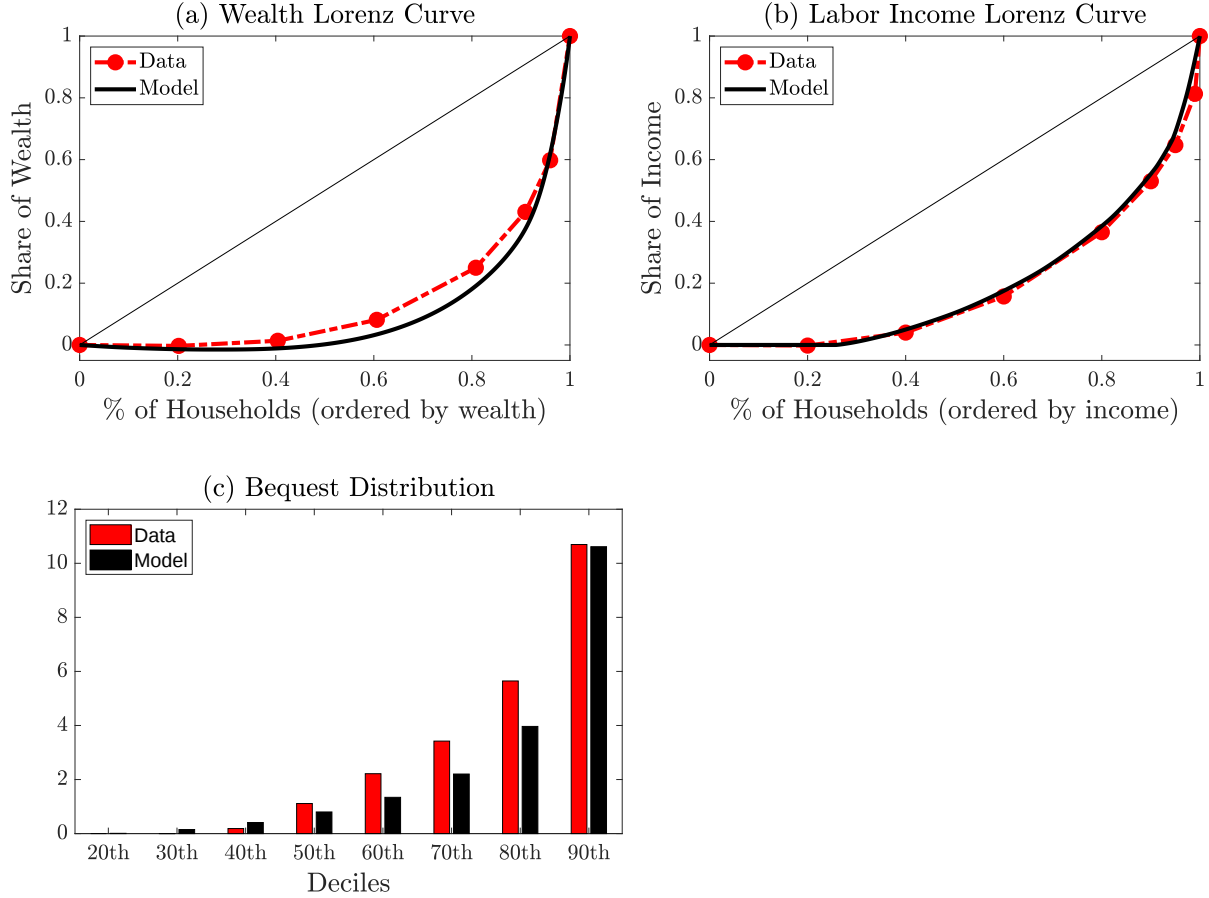
3.2 Baseline Economy

The model matches the set of targeted moments very closely, as shown in [Table 2](#). Next we examine the fit of the model against a set of moments that we did not target in calibration. To do so, we construct empirical counterparts to objects in the model to be consistent with a household concept, using the Consumer Expenditure Survey for household consumption expenditures, the Panel Study of Income Dynamics (PSID) for household labor income and hours, and the Survey of Consumer Finances (SCF) for wealth.

First, [Figure 1](#) examines the aggregate distributions of wealth and labor, as well as the distribution of bequests from households over the age of 70. Although the model is calibrated to match a sparse set of distributional moments (the share of wealth above and below the 80th percentile, the share of labor income to the top 20%, the average bequest and the share of bequests left by households at the 90th percentile of the bequest distribution), it characterizes the whole distribution in each case. Panel (a) shows that the model's wealth Lorenz curve matches the data quite well over the entire wealth distribution,²³ panel (b) shows that the model closely matches the Lorenz

²³A well known feature of this class of models is a tendency to underpredict the amount of concentration at the very top of the wealth distribution. Because the model was calibrated to capture wealth inequality in the top 20% of the distribution and we did not construct the model to capture the extreme skewness in the top 1% of the wealth distribution, we exclude the top 1% from both the model and the data in the depicted comparison. We calculate wealth as the households' net worth from the

Figure 1: Wealth and Bequest Distributions, Model and Data



curve for labor income; and panel (c) shows that the model matches the distribution of bequests quite well.²⁴

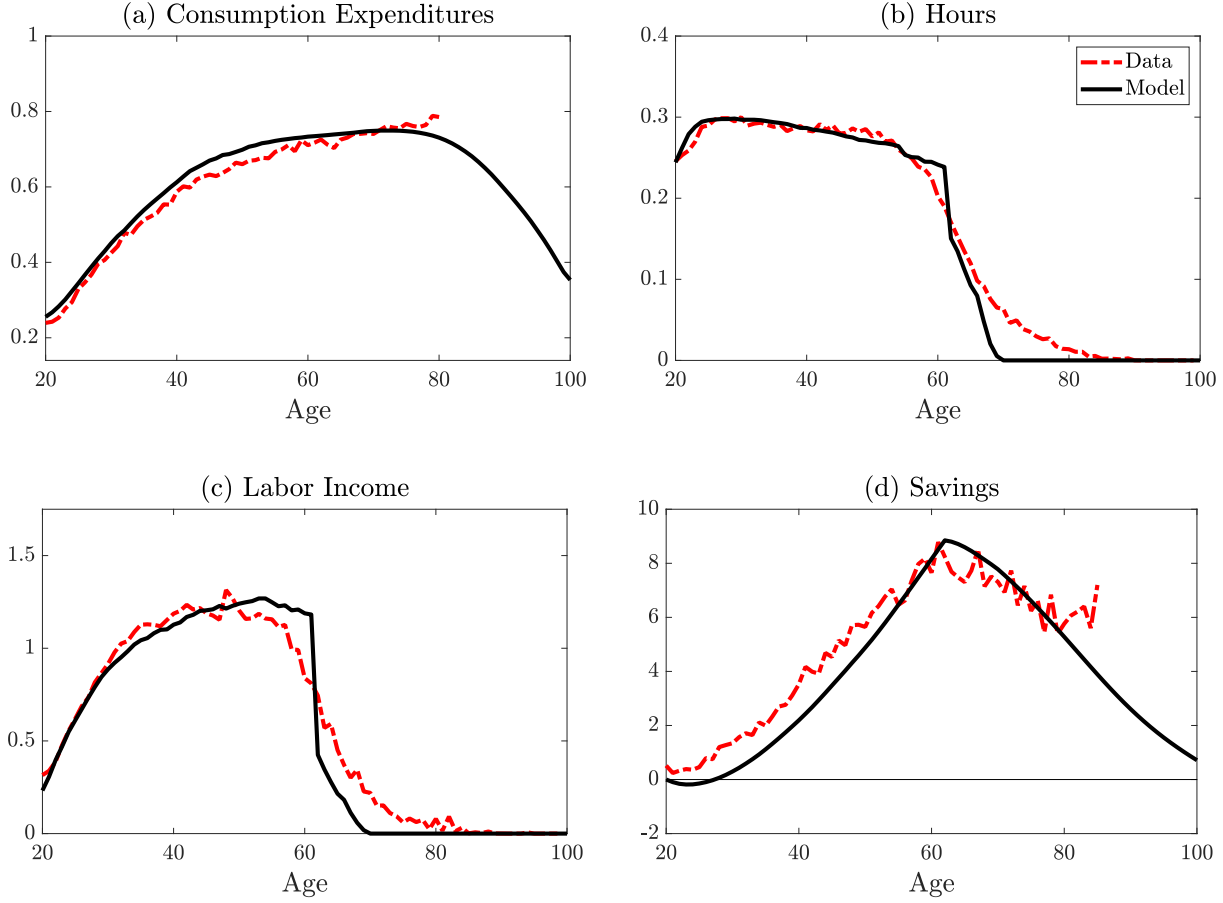
Next, because the evolution of households' allocations along the life cycle will be a key determinant of the effects of fiscal policy, we check the model's fit against the life cycle profiles of average consumption, savings, labor income, and hours by age in [Figure 2](#). In panel (a), we find that consumption in the model matches that in the data over the available range of ages, both in terms of contour and level.²⁵ Likewise, from

2016 Survey of Consumer Finances.

²⁴We calculate bequests from the Health and Retirement Survey (HRS) which samples households over the age of 70. In order to focus on bequests that are not transferred within the household, we exclude estates in which there were assets transferred to the spouse.

²⁵We follow [Aguir and Hurst \(2013\)](#) in measuring the relevant empirical counterpart to the model's consumption expenditures as total household consumption expenditures including primary and owner equivalent rents, and excluding durable goods expenditures, work related expenses and education. We further exclude medical expenditures as these are explicitly modeled for post-retirement households. We measure consumption expenditures for head of households of ages 20-80, and estimate age profiles with cohort fixed effects, normalized year fixed effects, and controls for education

Figure 2: Life Cycle Profiles, Model and Data



Notes: Solid lines depict the model's life cycle profile under the baseline public debt policy (67% of output). Dashed lines depict empirical life cycle profiles. Hours profiles are normalized by total annual hours. All other model generated life cycle profiles are normalized by the model's aggregate labor income and empirical life cycle profiles are normalized by PSID aggregate labor income.

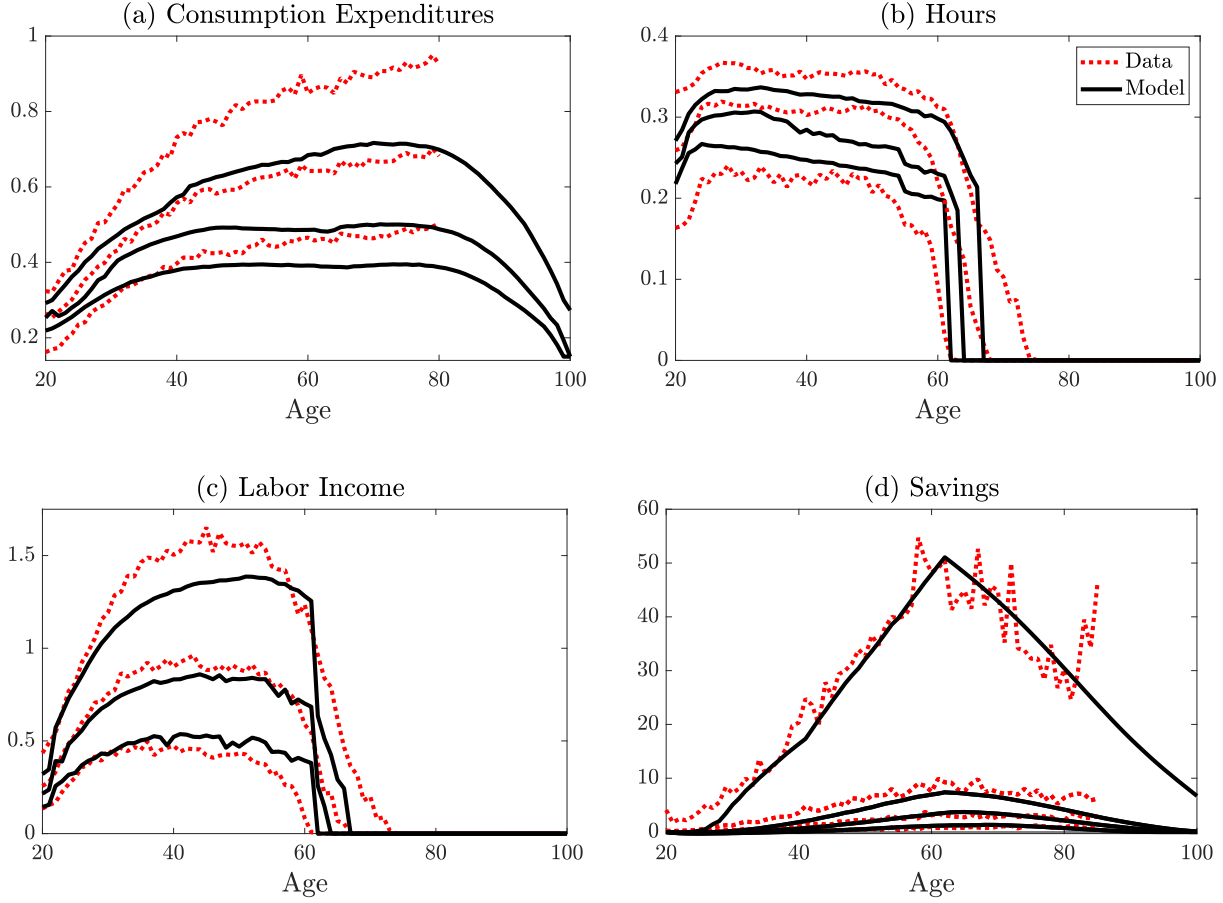
panels (b) and (c), average household hours and labor income in the model are very close to those in the data at each age.²⁶ Lastly, panel (d) demonstrates that the model generates a very good match to the empirical life cycle profile for average savings.

Finally, in [Figure 3](#) we assess how well the model characterizes the dispersion in consumption, savings, labor income and hours over the life cycle by comparing the

and sex of the head of household. Consistent with [Aguiar and Hurst \(2013\)](#), we do not include later ages due to a small sample in the Consumer Expenditure Survey. We express consumption expenditures as a fraction of aggregate labor income in the model and in the PSID.

²⁶We measure hours worked and labor income from the PSID. Household hours are calculated as the annual hours worked by the head of household and a spouse (if any), normalized by total annual hours (40 hours per week times 52 weeks per year) and the number of earners within the household (1 or 2). To be consistent with the PSID which topcodes labor income reports, panel (c) compares the data to the bottom 99% of labor income observations in the model.

Figure 3: Distribution of Life Cycle Profiles, Model and Data



Notes: Red dashed lines depict data percentiles (25th, 50th, 75th) that have been normalized by PSID aggregate labor income. Black solid lines depict model percentiles (25th, 50th, 75th) that have been normalized by model generated aggregate labor income. The hours profile was normalized by total annual hours. The savings profile has an added 97.5th percentile on top of the 25th, 50th and 75th percentiles.

25th, 50th, and 75th percentiles at each age in the model and data. Although the model does not explicitly target the dispersion in household allocations by age, it generates a reasonably close fit to its empirical counterparts, particularly for hours, labor income and savings. Additionally, given the skew in the wealth distribution, we examine the top of the distribution and show savings at the 97.5th percentile of the distribution by age also fits the data well. Although the model underpredicts the levels of consumption at these percentiles, which implies a more skewed consumption distribution in the model, it still captures well the rise in consumption dispersion relative to the median over the life cycle.

Overall, the model describes the data well. We find that the model not only has a tight in-sample fit, but also matches a large number of untargeted moments that

characterize life cycle averages, aggregate inequality and how inequality evolves over the life cycle.

4 The Effect of Public Debt-Financed Policy on Interest Rates

Given a model that is calibrated to recent U.S. data on households and macroeconomic aggregates, we now measure the response of interest rates at varying maturities (horizons) to changes in fiscal policies that add to the public debt. We begin in [Section 4.1](#) by conceptualizing the mechanisms by which public debt affects interest rates. Next, in [Section 4.2](#) we consider a series of unanticipated one-time shocks in order to quantify mechanisms for different types of policies. We then measure the dependence of the interest rate elasticity on the level of initial debt, in [Section 4.3](#). Finally, in [Section 4.4](#), we feed a series of shocks into the model that match the size and composition of accumulated public debt since 2000 relative to the Congressional Budget Office projections (see [Committee for Responsible Federal Budget \(2024\)](#) for a description of the methodology). [Section 4.5](#) contains a series of robustness checks to validate our results.

4.1 Discussion of Mechanism

Before proceeding to quantitative results, it is useful to conceptualize the mechanisms by which public debt affects the interest rate. To start, we focus on the standard comparative static prediction that public debt crowds out the stock of capital held by private firms. The reasoning for this mechanism follows from the asset market clearing condition $A_t = K_t + B_t$, that equates the stock of household savings A_t with the demand for those loanable funds by both firms in the form of private capital K_t and the government in the form of public debt B_t .

There are two channels that affect the size of this crowd out. First, holding household savings constant, if the government increases its demand for funds by dB units then there are mechanically dB fewer units available to private firms as private capital. Thus, an increase in public debt to $B_t + dB$ reduces the economy's amount of private capital to $K_t - dB$. Such a reallocation of private capital away from firms increases the marginal productivity of an additional unit of capital and thus firms are willing

to pay a higher interest rate, r_t , to households,

$$\frac{dr_t}{dB_t} = -\frac{dr_t}{dK_t} > 0 .$$

This mechanism illustrates the *direct crowd-out channel* by which public debt exerts upward pressure on the interest rate.

While the first channel characterizes a partial equilibrium effect on the interest rate, the second channel derives from the general equilibrium response of household savings to increase debt. Representing the amount of private capital that is crowded out by an increase in public debt by dK_t/dB_t , we can rearrange the asset market clearing condition $K_t = A_t - B_t$ to derive the change in the interest rate from an increase in public debt when household savings responds,

$$\frac{dr_t}{dB_t} = \underbrace{\left(\frac{dA_t}{dB_t} - \frac{dB_t}{dB_t} \right)}_{\equiv dK_t/dB_t} \cdot \frac{dr_t}{dK_t} .$$

The expression $dK_t/dB_t = dA_t/dB_t - 1$ indicates that the change in private capital is derived from the response of household savings to increased public debt dA_t/dB_t , in addition to the standard direct crowd-out channel represented by $-dB_t/dB_t = -1$. If household savings were to increase in response to increased public debt, $dA_t/dB_t > 0$, as would naturally be the response to a higher interest rate arising from the direct crowd-out channel, the increase in loanable funds to firms mitigates the crowd-out of private capital and thus the interest rate may increase by less. We call this the *savings channel* by which public debt exerts downward pressure on the interest rate.

Importantly, the strength of the savings channel need not be constant as it could, for example, depend on the initial level of debt. In particular, as debt increases, the strength of the savings channel could decline as households accumulate more savings.²⁷

While the previous reasoning applied to a comparative static on long-run outcomes, the effects of the savings channel need not be constant over time as the economy transitions to a new steady state with higher public debt. Particularly, the transition dynamics of the interest rate could critically depend on the type of fiscal policy and whether (and how) that policy directly impacts households' savings decisions,

²⁷The overall response of interest rates to increased public debt depends on the degree of diminishing marginal returns to an additional unit of capital and the magnitude of the savings channel. Generally, for a comparative static on long-run outcomes, the savings channel will be bounded between zero and one, e.g., $0 < dA_t/dB_t < dB_t/dB_t = 1$.

Table 3: Interest Rate Elasticity With Respect to Public Debt-to-Output

Counterfactual	Yields*		Forward Rates*		New
	10yr	30yr	5yr/10yr	10yr/10yr	Steady State
Higher Gov. Spending	2.53	2.09	2.32	2.02	1.64
Lump-Sum Transfer	0.61	1.19	1.19	1.39	1.64
Tax Reduction	0.03	0.68	0.16	0.72	1.64

Note: () Yields and forward rate elasticities are calculated as of the time of the debt-financed fiscal policy shock.*

since the fiscal policy can have a substantial effect on the savings channel over the transition. For example, an increase in public debt that finances lump sum transfers to households will result in a significant savings channel as households save a large portion of the transfer to afford a higher level of lifetime consumption. By boosting household savings, the lump sum transfer exerts downward pressure on the interest rate and slows its growth toward its new steady state value. In contrast, an increase in public debt that finances government expenditures does not directly boost household savings. Instead, households respond to a higher interest rate caused by the direct crowd-out channel by gradually increasing their savings, which generates a weaker savings effect as the interest rate slowly declines toward its new steady state value.

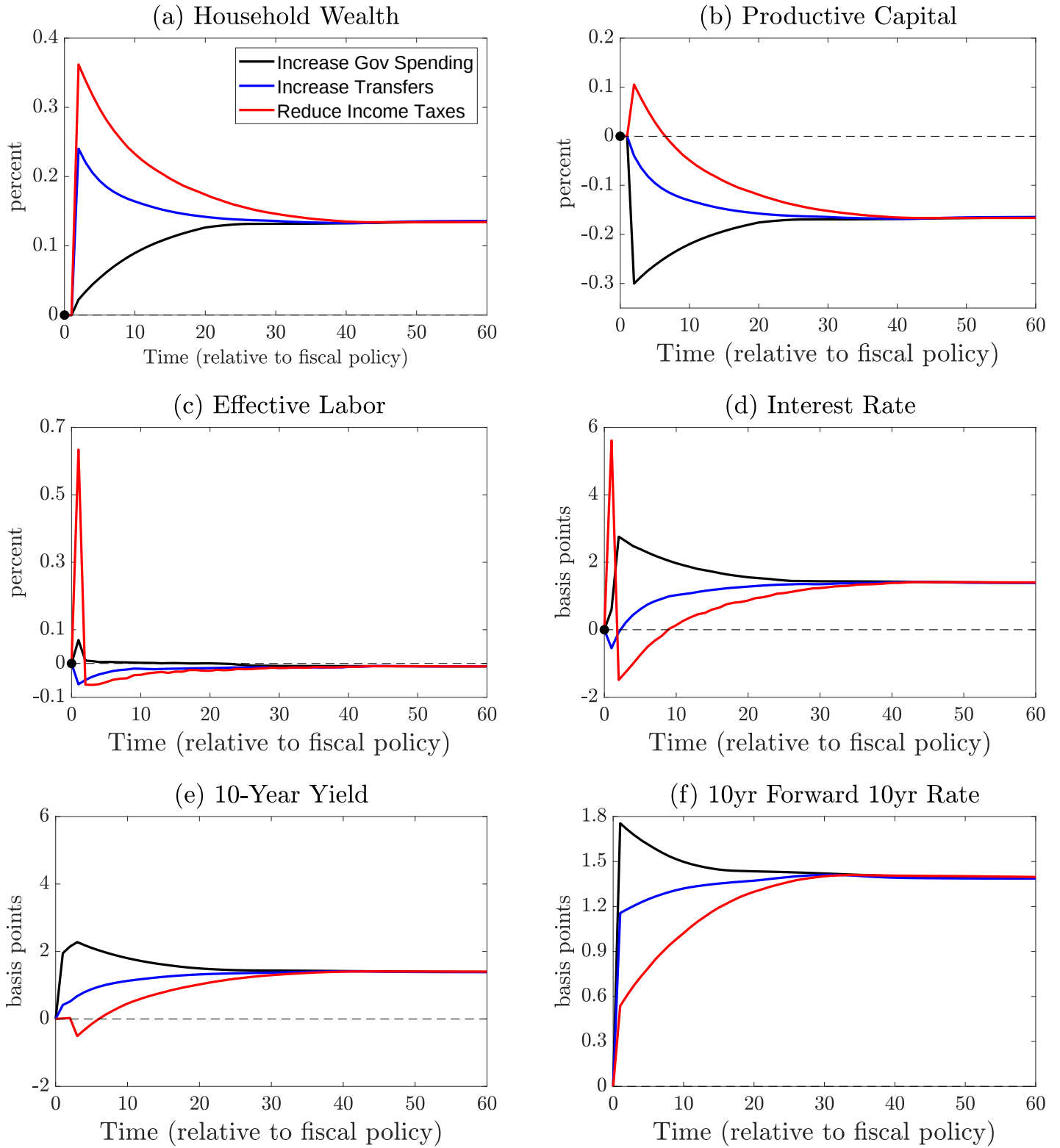
4.2 Variation in Interest Rate Elasticity by Policy Type and Over Time

Given the potential variation in the interest rate response to the fiscal policy, both across policies generating the debt and over time, we consider the implications of (i) a one time increase in government spending, G , (ii) a one-period decrease in the linear component of total income taxes, τ_0 of the tax function $Y(y_j(h, a, e, d))$, and (iii) a one-period increase in lump-sum transfers that are equally distributed across households, Tr . All three experiments assume fiscal shocks that generate a 2 percentage point increase in public debt relative to the initial level of output, so that each economy converges to the same steady state with 2 percentage points higher debt.²⁸

In the new steady state equilibrium, the interest rate is 4.6 basis points higher which implies a long-term elasticity of interest rates with respect to government debt of 1.6 basis points. However, [Table 3](#) reports the large dispersion in the elasticity on

²⁸We choose the shock magnitude of 2 percentage points since that is the average annual increase in the public debt to GDP ratio over the relevant time period.

Figure 4: Transition Paths for One-Time Debt Increases



rates at the time of the shock. For example, while past research estimates a singular elasticity of long rates using the 5-year forward, 10-year interest, we find that there is a large amount of variation in the elasticity depending on the policy: 2.3 basis points when the debt is generated from government purchases, 1.2 basis points when it is generated from a lump-sum transfer, and 0.2 basis points when it is generated from a tax cut. As panel (d) of [Figure 4](#) shows, the dispersion in the elasticities is generated by distinct dynamic transition paths of the one period interest rate across the policy experiments.

The variation in the elasticity primarily depends on whether the government uses the debt to provide a windfall to households or uses it for government consumption. For example, public debt-financed government expenditures do not directly transfer resources to households, and so household savings barely responds at the time of the fiscal policy shock and there is essentially a one-to-one crowd out of productive capital that induces a higher interest rate (see the black lines in panels (a), (b) and (d) of [Figure 4](#)). Over time, households respond to the higher interest rate by accumulating savings which puts downward pressure on the interest rate. All told, the total increase in household savings is less than the increase in government debt, and thus the interest rate settles at a higher level than in the initial steady state. Because the amount of productive capital crowd-out between years 10 to 20 is higher than in the new steady state, the estimated elasticity on the 10-year interest rate is 2.5 basis points, almost one basis point higher than the steady state elasticity of 1.6 basis points. Similarly, the 5-year forward 10-year rate, the 10-year forward 10-year rate, 30-year yield elasticities are larger than the elasticity on the steady state rate. Moreover, because the initial increase in short rates retraces over time, after onset of the shock, there is downward pressure on interest rates going forward.

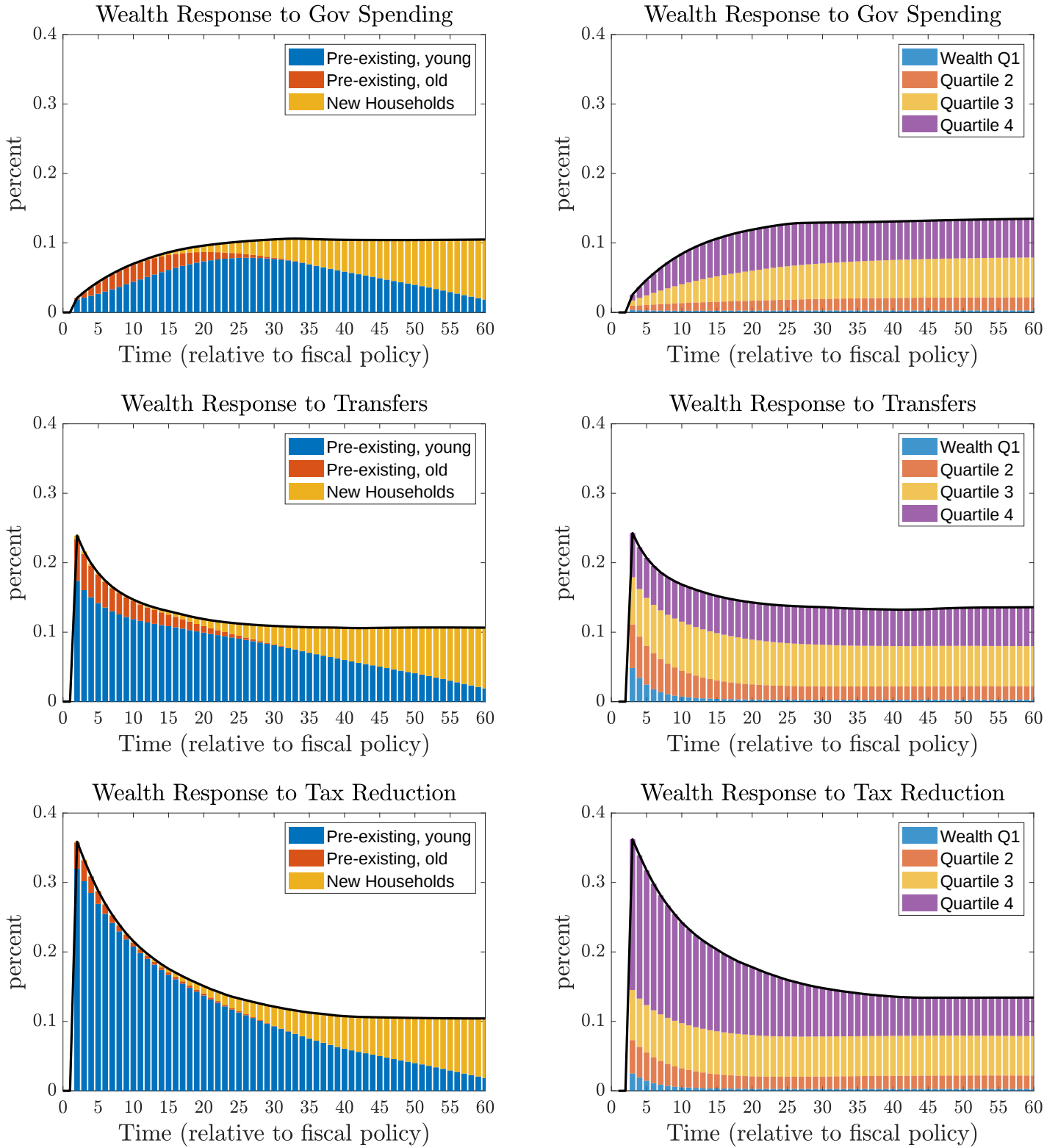
In contrast, when the higher debt finances a one period transfer to households there is a *crowd in* of productive capital since households receive a one-time windfall of the resources that generate the debt (see the large increase in the blue line of panel (a) of [Figure 4](#)). In total, since households initially save almost all of the windfall, the productive capital stock does not change much, which implies little immediate effect on the equilibrium interest rate. However, over time households spend down this windfall leading to a fall in productive capital and an increase in the equilibrium interest rate. Since it takes many periods for households to spend their elevated level of savings, the interest rate does not reach the new equilibrium for over 20 years, leading to a much smaller elasticity on the forward and long interest rates. Moreover, because the interest rate eventually reaches the same level in the steady state, there is still considerable upward pressure on long rates after the onset of the shock that

materializes over the next several decades.

To further illustrate the sources of the distinct transitions, we decompose the change in aggregate wealth over the transition paths into contributions arising from age and from position in the wealth distribution. The left-hand side panels of [Figure 5](#) decompose the deviation of wealth from the initial steady state, at every year in the transition, into contributions from households that enter the economy after the fiscal shock ("New Households"), households alive and under age 62 at the time of the shock ("Pre-existing, young"), and those that were alive and over 62 years old at the time of the fiscal shock ("Pre-existing, old"). The right-hand side panels decompose the change in wealth by quartiles of the wealth distribution. The top left panels demonstrate that after the government spending shock, initially younger households (who are still working) typically increase their savings. Moving forward, new households enter who also tend to save more. Over time, the households who were alive at the time of the shock die, and the size of the overall response is dominated by these new households' behavior. The top right panel demonstrates that the gradual increase in savings is mostly due to the households in the top half of the wealth distribution. In contrast, debt-financed transfers induce a larger initial increase in wealth across households of differing age and wealth, which is notably proportional to each group's share of the population, owing to the fact that these transfers are equally distributed to households (see the middle panels). Over time both the low-wealth households and households who were young at the time of the shock dissave their windfall which drives the subsequent reduction in wealth.

Finally, when the public debt finances a one-time tax cut, the transition dynamics are more similar to those with a transfer, but the interest rate elasticities are even more muted. The smaller initial elasticities occur because there is a second force leading to even more *crowd in* of productive capital. In particular, since households experience a one-period income tax reduction, they substantially increase their effective labor supply (see panel (c) of [Figure 4](#)) and save the resulting additional income for future consumption – on top of the savings from receiving the windfall of resources that generate the debt. In total, the additional crowd in leads to a larger productive capital stock relative to the initial steady state, thus pushing down the equilibrium interest rate. The bottom panels of [Figure 5](#) show that the additional accumulation of wealth derives from the responses of younger workers and higher wealth households. Since these types of agents take even longer to spend their elevated level of savings, the interest rate 10 to 20 years after the tax cut is lower than its initial steady state value, leading to roughly no effect on the 5-year forward, 5-year interest rate and 10-year yield and a smaller elasticity on the 10-year forward, 10-year rate and 30-year yield

Figure 5: Decomposition of Wealth Response to One-time Debt Shocks



relative to the steady state elasticity (see [Table 3](#)). Importantly, because the interest rate increases over the transition, after the onset of the shock, there is still considerable upward pressure on long rates that materializes over the next several decades.

Taken as a whole, the dispersion in transitional responses to fiscal shocks indicate that the “interest rate elasticity with respect to public debt” is not a well-defined object. The long transitional paths after each type of fiscal shock makes standard steady state comparisons misleading for policy analysis within standard planning periods (e.g. 10 to 20 years). Importantly, fiscal policies that transfer resources to households lead to quite different savings and interest rate dynamics than fiscal policies that do not allocate resources directly to the households. Thus, these results indicate that one must consider the timing and source of the debt to fully understand the imprint of debt on interest rates. Moreover, it is important to recognize that, even after the debt has been realized, the debt shock can still impose dynamic forces on long interest rates causing them to either increase or decrease depending on the type of policy that created the debt.

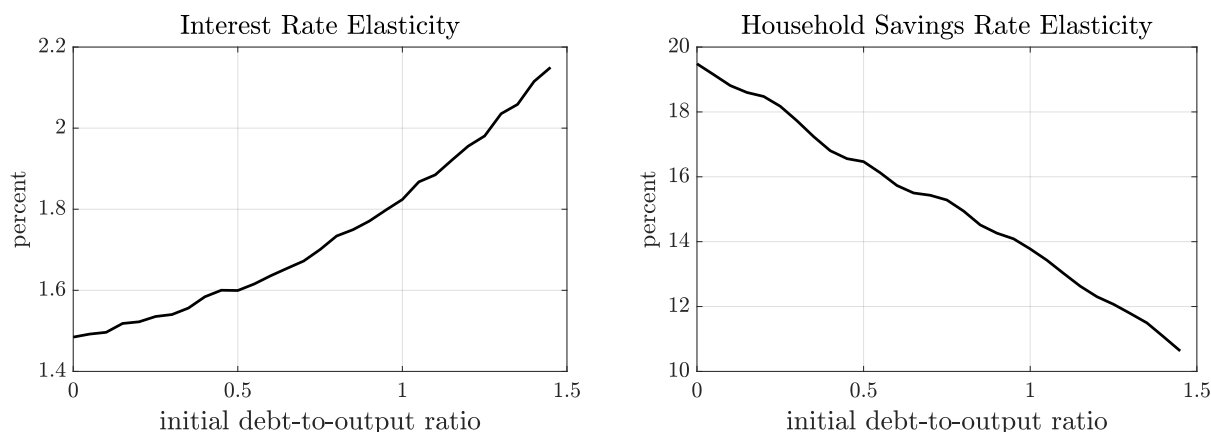
4.3 Debt Level Effect on the Interest Rate Elasticity

Next, given the large run up in debt over recent history, we consider the relationship between the long run interest rate elasticity with respect to an increase in government debt and the the initial level of debt. The left-hand panel of [Figure 6](#) plots the interest rate elasticity for progressively larger initial debt-to-output ratios, and the elasticity is increasing with the initial levels of debt. A higher level of public debt results in a larger stock of households savings in the initial steady state. Thus, an additional unit of savings is less valuable to households and, in turn, households are less responsive to increases in the interest rate. All told, the strength of the savings channel declines for higher levels of initial debt (plotted in the right panel) leading to more capital crowd out and a larger interest rate elasticity.

4.4 The Effects of Historical Debt Accumulation on Interest Rates

Our results imply that the effect of increases in government debt on interest rates depends on the level of debt at the time of a policy change, the type of policy that increases the debt, and the time elapsed since policy enactment. Given these results, we next use our model to inform our understanding of the interest rate effects of debt accumulation over the past 25 years. To do so, we feed the last 25 years of fiscal policies through our model. Importantly, the goal of this exercise is to isolate

Figure 6: Interest Rate Elasticity by Initial Debt-to-Output Ratio



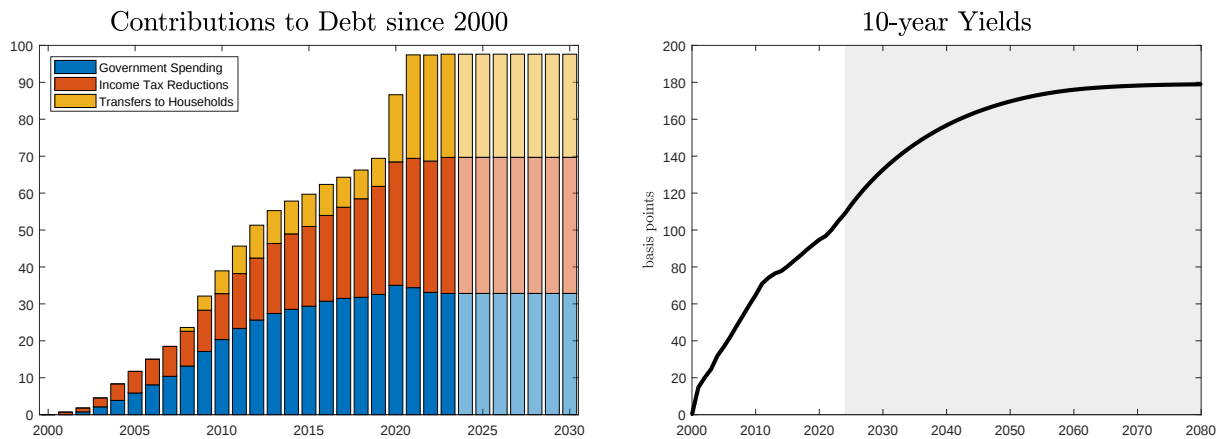
the effects of the debt accumulation and, therefore, we purposely abstract from the numerous other factors that affected interest rates over this period (e.g. population aging and the global savings glut).

We quantify the shocks to debt since 2000 as deviations relative to the Congressional Budget Office's expectations at that time. We decompose the changes in debt into components that are due government spending, income tax cuts and transfers to households based on [Committee for Responsible Federal Budget's \(2024\)](#) estimates.²⁹ Figure 7 shows the decomposition. First note that the decomposition shows debt as a percent of GDP is 100 percentage points higher as of 2023 than the Congressional Budget Office would have expected it to be in their 2000 baseline projection. At the beginning of this period, policy changes that increased government purchases were largely responsible for growing debt. Tax cuts also notably led to further debt accumulation, particularly since 2010. Transfers most notably played a role in the accumulation of debt in two specific episodes: during the Great Recession and particularly in response to the COVID-19 pandemic. Finally, for this simulation, we assume that there is no further growth in debt accumulation after 2023, as indicated by the constancy of the light shaded bars in Figure 7.

Figure 8 plots the transition path for an economy in which there is 100 percentage points of incremental debt that follows the composition and timing in the upper left figure. The black line in the upper right panel traces out the effect of this debt on the 10 year interest rates over time. Initially the 10 year yield jumps up by 20 basis points because of two factors. First, the incremental debt in the beginning is largely due to an increase in government purchases which generates a larger elasticity on the

²⁹We treat the debt increases due to policy actions in response to recessions as transfers.

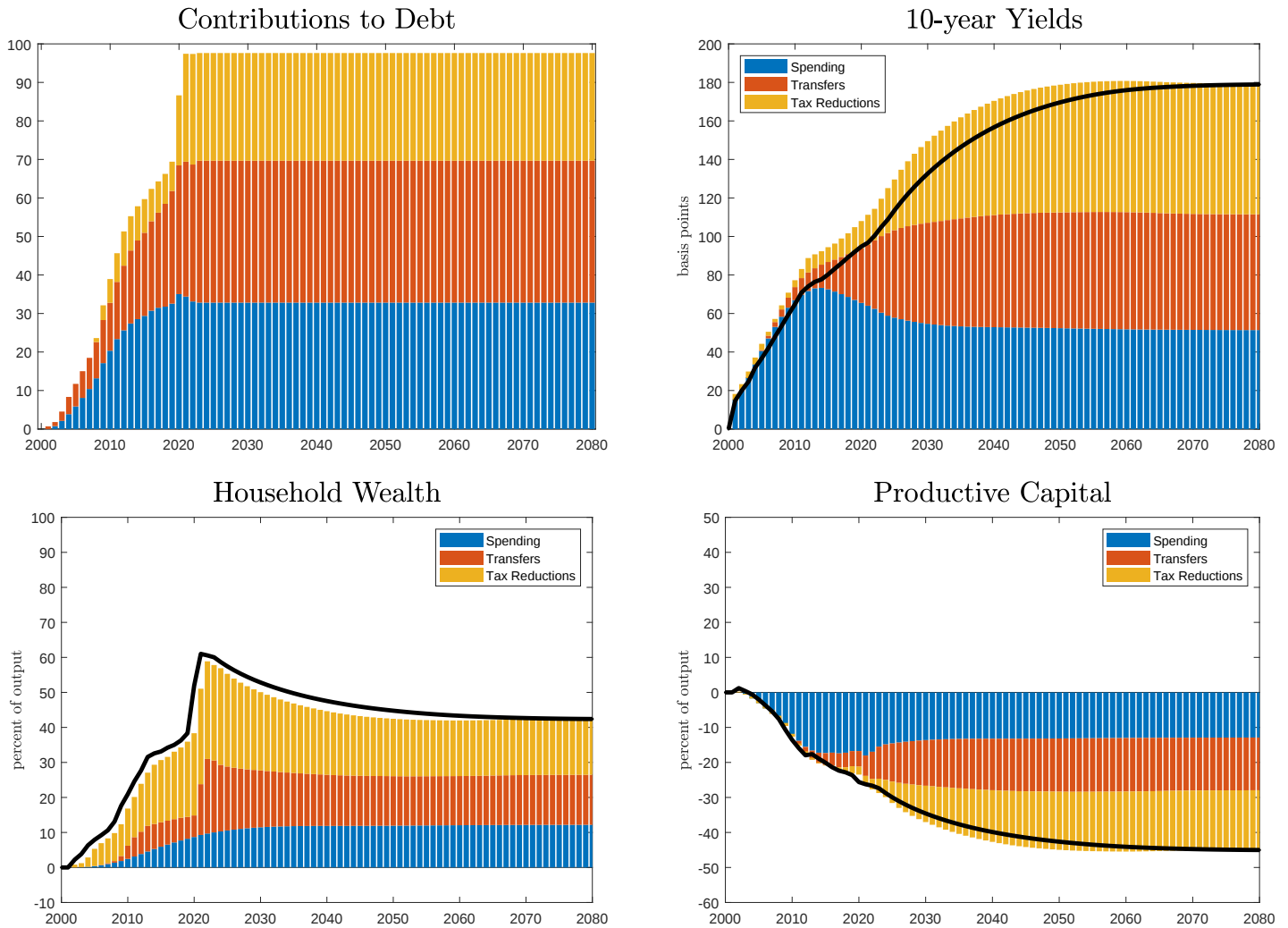
Figure 7: Debt Accumulation From Change in Path and Interest Rate Response



interest rate at the time of the shock. This point is illustrated by the bars in the upper right panel which decomposes the effects on the interest rate from the three types of debt shocks. Because the initial effect on interest rates from government purchases is larger than the eventual steady state effect the contribution to the interest rates from government purchases (the blue bars) peaks after 12 years and starting in 2012 the upward pressure starts to recede. Second, the simulations assume perfect foresight for the path of debt, so the 10 year interest rate reacts to the effects of not just the incremental debt in the first year but the whole future path of debt. Importantly, we demonstrate in [Section 4.5](#) that anticipated changes in debt more than ten years in the future do not have material effects on the 10 year interest rate beforehand. In particular, households' savings and labor adjustments in response to anticipated changes in debt have a limited effect on the spot rate. Instead, the initial increase in the 10 year interest rate is almost entirely due to the anticipated increases in debt over the next ten years and how those changes affected the spot rate within the 10-year window. Thus, the immediate jump in the interest rate is also due to the household incorporating the total increase in debt over the first ten years all in this first period. After the initial increase, the delayed effects of the tax cuts start to build, leading the interest rate to continue rising. Nevertheless, as of 2023, even though there is no more accumulated debt in the simulation, only 100 bp of the total 180 bp points has been phased into the 10 year interest rate. It takes around three more decades for these full effects to completely phase in.

This result, that the equilibrium interest rate continues to rise for a protracted period after debt has stopped growing, matters for policy determination. For example, the result implies the rise in future borrowing costs due to previously accumulated

Figure 8: Transition Paths for 2000-2023 Debt Accumulation



public debt has only been partially realized, and therefore predictions about the sustainability of U.S. public debt would be too optimistic. Similarly, all else equal, an increasing equilibrium rate may be an important benchmark when setting monetary policy over this period.

4.5 Robustness

In this section we consider several extensions to the economic environment presented above in order to gauge the degree to which our results depend on assumptions about information and savings behavior.

Anticipatory Effects. The previous exercises assumed perfect foresight after an un-

Table 4: 10yr Yield Elasticity to an Pre-Anounced Policy Change

	11yr Ahead	5yr Ahead	Long Run
Higher Gov. Spending	0.0	0.8	1.6
Lump-Sum Transfer	0.1	—*	1.6
Tax Reduction	0.0	0.4	1.6

Note: () Computations forthcoming.*

expected initial shock. However, economic policies are largely enacted after public debate and have both predictable and unpredictable components. Accordingly, we now relax the assumptions on information.

We consider how the interest rate reacts to an announcement about debt-financed policies. Importantly, future debt affects the ten year yield – which is the average of the one period risk free return over the next ten model periods – through two channels: (a) households may react to the anticipated debt which leads to changes in the current one year interest rate, and (b) if additional debt is accumulated within the next ten years, that could have direct effects on the future spot rates within the ten year window. To gauge the magnitude of the first channel in particular, we simulate a debt shock from the three policy types that are announced today but do not take affect for 11 years implying that any of the immediate effects on interest rates are from the this channel. In the first column of [Table 4](#), we estimate the elasticity of the 10 year interest rate to a debt shock that occurs 11 years in the future is essentially zero for all three policy shocks. In the second column, we estimate the effects on interest rates from the pre-announced policies when the policy change is 5 years in the future. We find that in this case, when the policy change is within the ten-year window, the interest rate does change however the effects do not filter into the whole ten year window.

Marginal Propensity to Consume. In the previous exercises, we find that the savings channel significantly influences the strength of the interest rate response to debt-financed fiscal policy and the interest rate dynamics over the transition to the economy’s new steady state. In particular, households took a significant amount of time to spend savings from policy windfalls or to build savings in the face of higher interest rates from increased government spending. Thus, the marginal propensity to consume will be an important determinant of interest rate dynamics, particularly in the case of lump sum transfers and tax reductions. Accordingly, we will now boost the model’s marginal propensity to consume by extending the model with an updated

Table 5: Interest Rate Elasticities and Foreign Investment Response to Debt

<i>Panel A</i>	No Foreign Response		
	10yr Yield	5yr/10yr Forward	Long Run
Higher Gov. Spending	2.53	2.32	1.64
Lump-Sum Transfer	0.61	1.19	1.64
Tax Reduction	0.03	0.16	1.64

<i>Panel B</i>	With Foreign Response		
	10yr Yield	5yr/10yr Forward	Long Run
Higher Gov. Spending	2.13	1.99	1.42
Lump-Sum Transfer	0.18	0.83	1.42
Tax Reduction	-0.39	-0.21	1.42

notion of asset liquidity. In particular, suppose that a share of each agent's wealth plus borrowing capacity is fully liquid while a complementary share cannot be dissaved. Following Nakajima (2023) and Bayer et al. (2024) we generalize the standard liquidity constraint to incorporate variation in asset liquidity,

$$a_{j+1} - a_j \geq -\vartheta_j(a_j - \underline{a})$$

where we denote the liquid share of wealth plus borrowing capacity ($a_j - \underline{a}$) by $\vartheta_j \in [0, 1]$, which we allow to vary by age. Given the strong retirement savings incentives in the model, this liquidity constraint can be interpreted as enforcing illiquidity from tax-deferred retirement savings contracts (see Huntley and Michelangeli (2014)). Notice that this liquidity constraint embeds the baseline borrowing constraint when cash-on-hand is fully liquid (e.g., when $\vartheta_j = 1$) and imposes no dissaving when cash-on-hand is fully illiquid (e.g., when $\vartheta_j = 0$) so that $a_{j+1} \geq a_j$. We calibrate ϑ_j to the share of liquid assets in the Survey of Consumer Finances following asset definitions explained in Kaplan et al. (2014). Results from this robustness exercise are currently in-progress.

Foreign Investment. Finally, we check the sensitivity of the interest rate elasticities to the assumption that the level of foreign investment does not change with the level of debt. In particular, we calculate interest rate elasticities when foreign investment (F) increases proportionately to the increase in public debt.³⁰ In table Table 5, we find

³⁰In this exercise, we calculate the increase in foreign savings so that the *ratio* of foreign savings to public debt is held constant.

that the long run elasticity is modestly lower when the level of foreign investment increases with debt. Unsurprisingly, the lower elasticity reflects the greater amount of foreign funds offsetting some of the potential crowd out effect from the public debt. Dynamically, we also find that the reduction in crowd out leads to a smaller elasticity of interest rates at impact.

5 Estimating the Interest Rate Elasticity of Debt

Next, we relate the model results to empirical estimates of the response of the real interest rate to a change in public debt. Conceptually there are several threats to identification from naively regressing interest rates on measures of public debt, most importantly that the short-term the interest rate varies with macroeconomic conditions and shocks that are unrelated to variation in public debt. In order to purge our estimates of confounding shocks, we follow [Laubach \(2009\)](#) and [Engen and Hubbard \(2004\)](#) in using forecasted values of debt and medium-term forward interest rates, as well as including a large set of controls for other macroeconomic shocks that simultaneously affect debt and interest rates. Importantly, we update the standard approach by identifying elasticities from *forecast revisions* instead of forecasted levels of debt. One advantage of this strategy is that the evolution of government debt is plausibly non-stationary (c.f. [Barro \(1979\)](#), [Bohn \(1998\)](#), and [Campbell et al. \(2023\)](#)), while forecast revisions are stationary and thus estimates exhibit greater coefficient stability. Second, constructing forecast revisions allows us to isolate different spending sources that explain the change of public debt and test whether elasticity estimates are sensitive to these sources.

5.1 Methodology, Data and Estimates

Framework and Previous Estimation. The estimation framework proceeds from a standard government budget constraint. The government spends G_t and receives T_t in taxes from households each period, to form the primary surplus of $T_t - G_t$. The government chooses its level of new borrowing, D_t , and pays interest on existing debt at the prevailing interest rate, $r_t D_{t-1}$. We define debt as negative $D_t < 0$, but the government can also save by choosing $-D_t > 0$. Thus the government's budget constraint is,

$$D_t - D_{t-1} = (T_t - G_t) + r_t D_{t-1} .$$

Accordingly, j -period ahead expectations of public debt are obtained by cumulating the government budget constraint,

$$\mathbb{E}_t[D_{t+j}] = D_{t-1} + \mathbb{E}_t\left(\sum_{j=0}^J (T_{t+j} - G_{t+j})\right) + \mathbb{E}_t\left(\sum_{j=0}^J r_{t+j} D_{t-1+j}\right).$$

Laubach (2009) and Engen and Hubbard (2004) estimate the impact of the *level* of public debt relative to GDP, denoted Y_t , on the j -period ahead interest rate with the following specification,

$$r_{t+j} = \alpha + \beta \mathbb{E}_t[D_{t+j}/Y_{t+j}] + \gamma X_t + \varepsilon_t \quad (9)$$

where X_t is a set of time-varying controls for macroeconomic conditions that might confound the effect of debt-to-GDP on interest rates.

For this specification, the interest rate data we use in estimation consists of updated yield curve estimates from Gürkaynak et al. (2007) to derive the 5-year ahead forward interest rate on a 10-year treasury bond. For the debt measure, we either use the CBO's 5-year ahead forecast for total public debt-to-GDP. Additionally, we control for expected total PCE inflation to effectively estimate the effect on the real interest, projected GDP growth to adjust the interest rate for growth trends as is predicted by a standard Euler equation, and the dividend yield to control for the effect of equity returns on the interest rate. We further control for the stock of US Treasuries held by the Federal Reserve and the stock of US Treasuries held by foreign governments to control for composition of government debt.³¹ Our choice of control variables closely follows Laubach (2009) and Gamber and Seliski (2019), and thus our results will be comparable.

Column (1) of Table 6 shows that a 1 percent increase in total debt-to-GDP leads to an increase in the 5-year ahead, 10-year interest rate of 2.4 basis points. This estimate falls within the range of those found in Gamber and Seliski (2019), which uses a similar sample period of 1987 to 2017 as well as the same controls variables. However, column (2) shows that when we extend the sample endpoint from 2017 to 2020 the estimates become negative and small, which we find is robust to several specifications. The sensitivity of the estimate to the sample period is plausibly due to a unit root in the time series for both public debt and interest rates. Both panels of Figure 9 show that interest rates and debt have a secular trend with multiple regimes. Fig-

³¹Including the composition of debt across domestic and foreign sources helps alleviate concerns that the elasticity is driven by a global savings glut during this time period, as discussed in Bernanke (2005).

Table 6: Coefficient Stability Across Specifications

	(1)	(2)	(3)	(4)
5yr Total Debt	0.024*** (0.007)	−0.005 (0.009)	0.050*** (0.019)	0.048*** (0.017)
Dependent Variable	$r_t^{5,10}$	$r_t^{5,10}$	$\Delta r_t^{5,10}$	$\Delta r_t^{5,10}$
Controls	×	×	×	×
Output Gap	t+1-t+5	t+1-t+5	t+1-t+5	t+1-t+5
GDP Growth	t+5	t+5	t+5	t+5
Aging				
Sample period	1987-2017	1987-2020	1987-2017	1987-2020
N	89	95	89	95

Notes: The dependent variable is the 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

Figure 9: Interest Rates and Debt

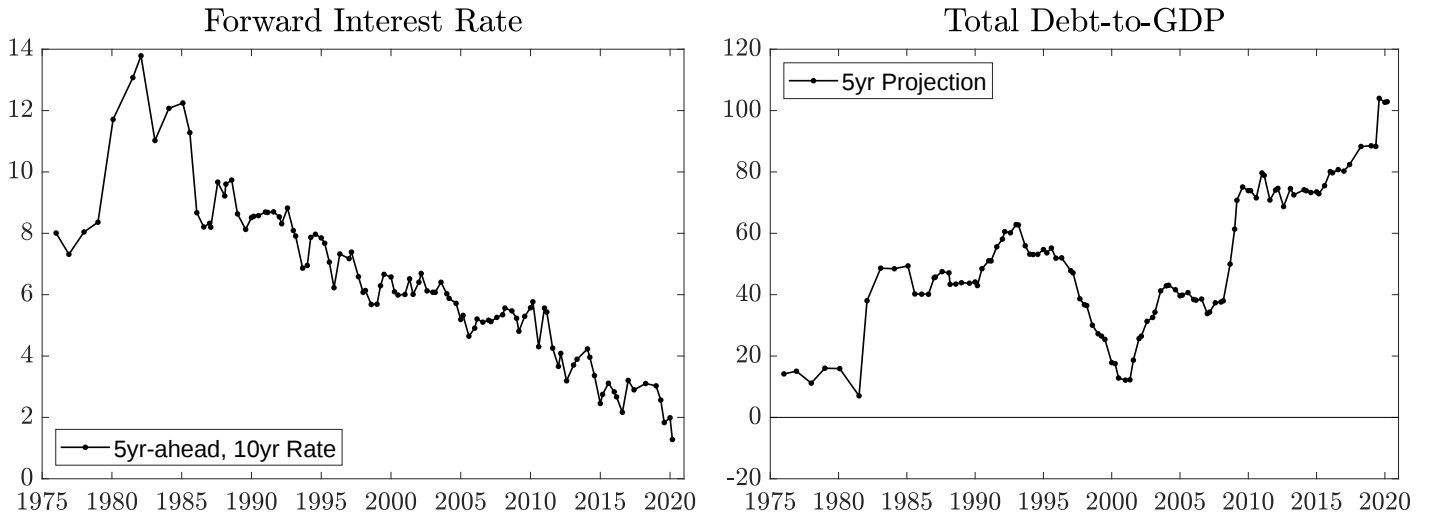
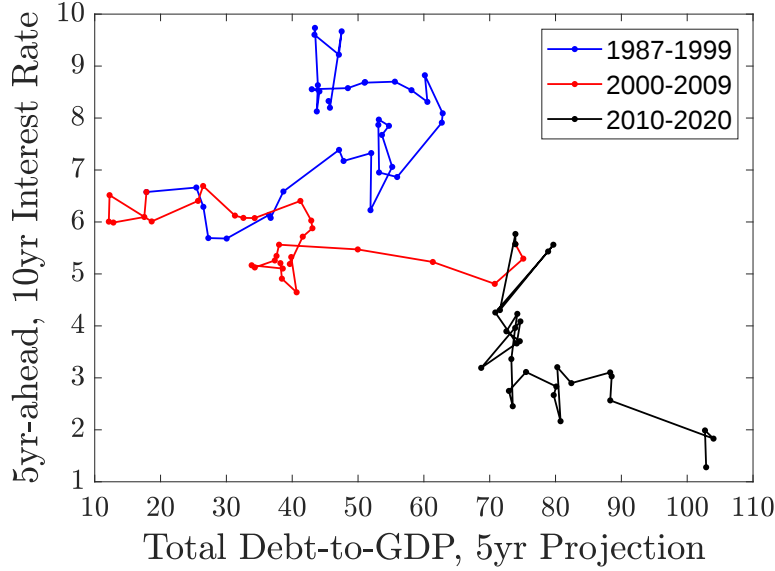


Figure 10 plots interest rates against expected public debt-to-GDP from 1987-2020 and breaks out three separate regimes: a positively relationship between 1987-1999, an essentially flat relationship between 2000-2009, and a negative relationship between 2010-2020. Importantly, we find that estimates fall considerably when the sample period is extended to include additional post-2010 data, which features a negative trend in interest rates and an upward trend in debt.

Baseline Specification. Our strategy for simultaneously introducing parameter sta-

Figure 10: Interest Rates and Debt Regimes



bility over sample periods and purging threats to estimation contained in short-term macroeconomic shocks is to consider a difference-in-difference style estimator that leverages information contained in successive forecasts. In particular, the j -period ahead forecast error is the difference between the expected debt and the actual realization of debt,

$$\eta_{t,t+j} = \mathbb{E}_t[D_{t+j}/Y_{t+j}] - D_{t+j}/Y_{t+j}$$

and the forecast revision is therefore the difference in forecast errors for date $t + j$ as of date $t - 1$ and as of date t ,

$$\Delta\eta_{t,t+j} \equiv \eta_{t,t+j} - \eta_{t-1,t+j} = \mathbb{E}_t[D_{t+j}/Y_{t+j}] - \mathbb{E}_{t-1}[D_{t+j}/Y_{t+j}] .$$

The primary distinction between the forecast at time $t - 1$ and time t is that the date t forecast contains additional information, and can thus be thought of as being the result of a treatment of additional information relative to the $t - 1$ forecast. Accordingly, we estimate the impact of the unexpected component of debt on the change in the j -period ahead interest rate, which gives the response of interest rates to news about debt, with the following specification,

$$\Delta r_{t+j} = \alpha + \beta \Delta\eta_{t,t+j} + \gamma \Delta X_t + \varepsilon_t \quad (10)$$

where ΔX_t is the first difference of the time-varying controls.

In addition to the control variables used in the levels specification in [Equation \(9\)](#),

we also control for any residual impact of the business cycle with the expected output gap from the CBO, to help absorb the effect of persistent business cycle shocks on public debt forecasts. Moreover, we control for supply side determinants of trend interest rates with a measure of population aging, specifically the ratio of the population over the age of 65 relative to that between ages 20 and 64.³² Finally, when the control variable is a forecasted value from the CBO (e.g., GDP growth and the output gap), we use forecast revisions as controls in this specification.

Before proceeding to introduce further aspects of the identification strategy, we assess the stability of the estimates derived from Equation (10). Columns (3) and (4) of Table 6 show that the updated specification yields estimates that are not sensitive to sample period, unlike the estimates in the specification in columns (1) and (2). Moreover, trends in the level data apparently attenuated the magnitude of the coefficient in half.

Endogeneity from Net Interest Payments. Next, given a strategy for identifying the effect of public debt on interest rates from the news contained in forecast revisions, we remain concerned that the way government debt is measured can threaten identification. In particular, one component of government debt is the net interest payment on existing debt, which contains interest rates from previous debt obligations. Thus, the component of net interest payments introduce a concern over reverse causality since those payments are a function of interest rates, and those interest rates may furthermore reflect a host of other shocks that are unrelated to the formation of the primary debt.

We address this concern by decomposing revisions to the total debt forecast into forecast revisions over the primary deficit and net interest payments. We do so by taking CBO deficit forecasts for the primary debt and net interest payments, which can then aggregate to debt forecast revisions over the projection horizon. We can subsequently study the primary deficit absent the plausibly endogenous component of net interest payments. This is a notable advantage of estimating in differences, as we do not need the *level* of debt due to the primary deficit or net interest payments but only the change in those components. This is precisely why prior work has not been able to separate the primary deficit from the net interest rate, empirical specifications in levels provide no way of separating debt projections into components.

In columns (1) and (2) of Table 7, we demonstrate that the potential bias from including net interest payments. We find that the estimate in column (1), which identifies the elasticity from total debt, is larger than the estimate in column (2) which

³²Controlling for population aging is consistent with work such as [Carvalho et al. \(2016\)](#) and [Acemoglu and Restrepo \(2017\)](#).

Table 7: Specifications in First Differences

	(1)	(2)	(3)	(4)
5yr Total Debt	0.048*** (0.017)			
5yr Primary Debt		0.041** (0.021)	0.042* (0.022)	
10yr Primary Debt				0.011 (0.012)
Dependent Variable	$\Delta r_t^{5,10}$	$\Delta r_t^{5,10}$	$\Delta r_t^{5,10}$	$\Delta r_t^{10,10}$
Controls	×	×	×	×
Output Gaps	t+1-t+5	t+1-t+5	t+1-t+5	t+1-t+10
GDP Growth	t+5	t+5	t+5	t+10
Aging	×	×	×	×
Sample period	1987-2020	1987-2020	1996-2020	1996-2020
N	95	95	68	68

Notes: The dependent variable is the 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

excludes net interest payments. Thus we find that excluding interest payments from the debt measure leads to somewhat smaller estimates, by around 7 basis points.

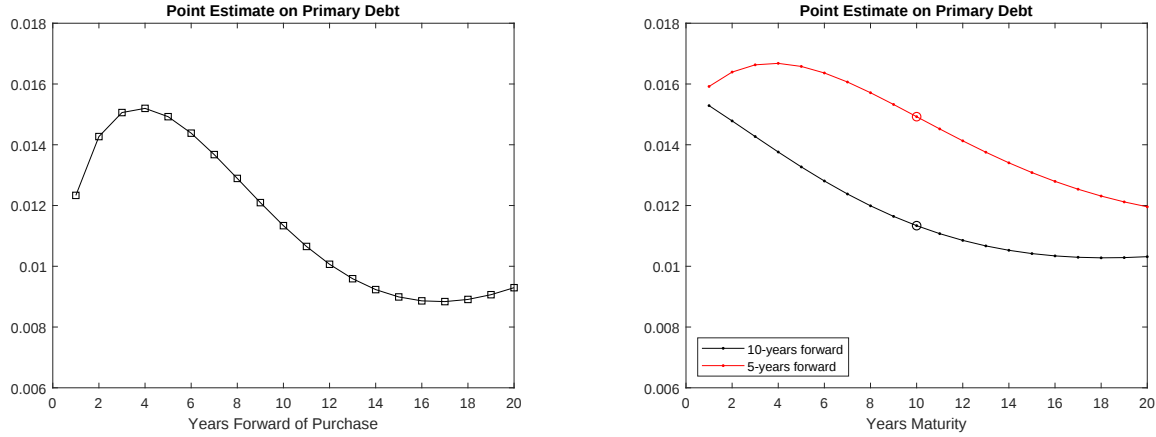
Forecast Horizon and Debt Maturity. The prior literature estimated effect of 5-year forward, 10-year interest rates on 5-year ahead public debt forecasts, and treated the 5-year horizon as a sufficiently close proxy to the long-run in which contemporaneous shocks could no longer contaminate the measures of interest rates and debt. In part, the choice of a 5-year ahead horizon was due to a data limitation, as the CBO only started forecasting at longer horizons in 1996.³³ We now turn to estimating our specification at a 10-year horizon, the longest horizon contained in post-1996 CBO projections, in order to obtain the elasticity of the 10-year ahead, forward interest rate on a 10-year bond with respect to the 10-year ahead forecast revision on the primary debt.³⁴

Columns (3) and (4) of Table 7 estimate the interest rate effect of higher public debt over the full ten year forecast horizon. Column (3) provides the specification with 5-

³³As an example, Laubach (2009) employs the sample period of 1976-2003, which did not include many observations with 10-year ahead forecasts.

³⁴We also include 10-year horizons for the relevant control variables, such as the changes in the GDP growth rate and output gap.

Figure 11: Local Projection of Interest Rates on 10-year Debt Projections



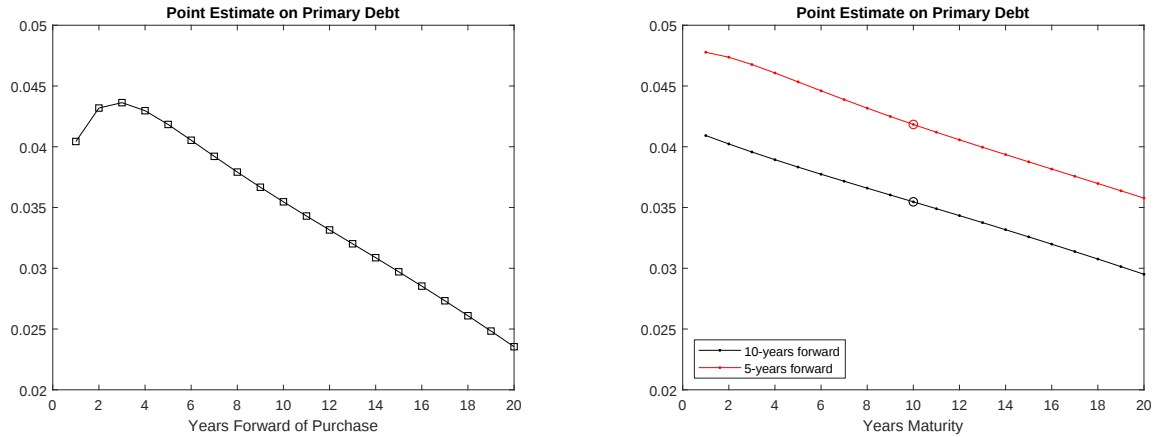
year primary debt projections from 1996-2020 as a benchmark for comparison. In column (4), when all ten years of debt information are included in the specification, we find a point estimate of 1.1 basis points.³⁵ It should not be surprising that the estimate is smaller at a longer horizon for public debt projections, since the magnitude of the change in forecasted debt over a longer horizon increases (e.g., since changes in annual deficits are persistent) but the dependent variable of interest rate changes has far less variation as we increase the number of years forward at which the bond is purchased. Mechanically, the point estimate falls as an independent variable with greater variance explains a dependent variable that has little changed.

Next, we show that the estimated elasticity varies with the particular forward rates that are used for identification. To do this, we consider a set of local projections of the interest rate with respect to the number of years forward that the bond will be purchased and the number of years the bond will be held. The left panel of Figure 11 shows that the elasticity with respect to 10-year the public debt projection declines as we increase the interest rate's purchase timing from 5-years forward to 10-years forward, while the left panel of Figure 12 shows that the elasticity with respect to the 5-year public debt projection is larger in magnitude and declines more rapidly. Likewise, the right panels vary the maturity of the bond and give a similar result.

Overall, the variation in the empirical estimates along both the years forward and the years to maturity are consistent with the results of our quantitative model experiments – that the effect of increased public debt on the spot interest rate is very persistent over the transition.

³⁵In robustness exercises with respect to specification, we find the coefficient that ranges between 1 and 1.4 basis points.

Figure 12: Local Projection of Interest Rates on 5-year Debt Projections



Elasticity Variation by Spending Source. Next, we show that the elasticity varies with the type of fiscal policy that generates the debt, which is consistent with the results from our quantitative model. In particular, we use the CBO’s forecast decompositions to construct forecast revisions for components of the primary deficit: government revenues (mainly inflows from taxation), mandatory government outlays (such as entitlement programs), and discretionary government outlays (mainly due to changes in annual budgeting as well as emergency legislation). We reestimate the empirical specification by replacing the 10-year forecast revision in the primary deficit with the forecast revisions in all three of its components. Table 8 shows that there is considerable heterogeneity in the elasticities with respect to (negative of) revenues, discretionary outlays and mandatory outlays.

In column (2) we find that the elasticity with respect to (the negative of) revenues is similar to, though somewhat larger than, the elasticity for the primary deficit as a whole (in column (1)). Moreover, the elasticity with respect to discretionary outlays is close to 1 basis point. The elasticity with respect to mandatory outlays is negative instead of positive, raising a concern that mandatory outlays could be correlated with the business cycle despite our experimental design to purge such correlation (e.g., since they include automatic stabilizer programs such as unemployment insurance or Medicaid). In column (3) we interact each component with a dummy variable that equals one when the 10-year projected output is below the 10-year projection for potential output, and only find a significant additional effect on the elasticity with respect to mandatory spending when the output gap is negative. Notably the additional effect on mandatory spending is positive, suggesting that households consume the increases in mandatory spending during downturns but save them otherwise, or that the forward rates are correlated with the cycle. Finally, we observe that the esti-

Table 8: Specifications with Debt Decomposition

	(1)	(2)	(3)
10yr Primary Debt	0.011 (0.011)		
10yr Revenues (neg)		0.021* (0.011)	0.020* (0.012)
10yr Discretionary Outlays		0.010 (0.025)	0.039 (0.052)
10yr Mandatory Outlays		-0.103** (0.050)	-0.158*** (0.050)
10yr Revenues $\times \mathbf{1}[gap < 0]$			-0.017 (0.025)
10yr Discretionary $\times \mathbf{1}[gap < 0]$			-0.053 (0.064)
10yr Mandatory $\times \mathbf{1}[gap < 0]$			0.118* (0.070)
Dependent Variable	$\Delta r_t^{10,10}$	$\Delta r_t^{10,10}$	$\Delta r_t^{10,10}$
Controls	$\times$	$\times$	$\times$
Output Gaps	t+1-t+10	t+1-t+10	t+1-t+10
GDP Growth	t+5	t+5	t+5
Aging	$\times$	$\times$	$\times$
Sample period	1996-2020	1996-2020	1996-2020
N	68	68	68

Notes: The dependent variable is the 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

mates are somewhat imprecise and not consistently statistically different than zero, in part given the relatively short time series. Overall, the considerable range of interest rate elasticities with respect to the subsequent increase in public debt are consistent with the quantitative model experiments which found that the elasticity is policy dependent.

6 Conclusion

In this paper we revisit the relationship between government debt and interest rates within a quantitative heterogeneous agent life cycle model. We find that the effects

of government debt on interest rates depends on the level of debt at the time of the increase, the composition of the debt-financed policies leading to the rise in debt, and how much time has passed since the debt was accumulated. the timing of these increases. Thus, we demonstrate that it is insufficient to characterize the relationship between debt and interest rates with one elasticity as is often done for policy making. Moreover, the type of policy not only affects the magnitude of the interest rate response at the time of the shock but can also lead to an increase or decrease in the interest rate after the initial response. Accordingly, we find that from the roughly 100 percentage points of additional debt accumulated since 2000 relative to CBO's expected path, just over half of the upward pressure on interest rates has been realized. These results imply that even without any additional debt accumulation, previously accumulated debt will still lead to an additional 80 basis points of upward pressure on interest rates over the next several decades. This prominent backloading of the effects of debt on interest rates suggests that, all else equal, the economy's capacity for debt sustainability may be overstated without taking these dynamics into account.

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Appendix

A	Robustness of Empirical Estimates	A-2
B	Construction of the Balanced Growth Path	A-5
B.1	Aggregate Conditions	A-5
B.2	Individual Conditions	A-7
B.3	Aggregation	A-8
C	Calibration	A-9

A Robustness of Empirical Estimates

The existing literature has noted that the interest rate elasticity with respect to public debt is somewhat sensitive to specification. As we showed, this is partially due to specifying the empirical relationship in levels. Here we check robustness around the specification for each of the features we introduce into estimation. We omit population aging throughout, focusing on the effect of the output gap in controlling for the persistence of business cycle shocks.

Table A1: Specification in Levels

	(1)	(2)	(3)	(4)	(5)
5yr Total Debt	0.020*** (0.008)	0.024*** (0.007)	−0.009 (0.008)	−0.005 (0.009)	−0.005 (0.009)
Dependent Variable	$i_t^{5,10}$	$i_t^{5,10}$	$i_t^{5,10}$	$i_t^{5,10}$	$i_t^{5,10}$
Output Gap	t+1		t+1		t+5
GDP Growth	t+5	t+5	t+5	t+5	t+5
Controls	×	×	×	×	×
Sample period	1987-2017	1987-2017	1987-2020	1987-2020	1987-2020
N	89	89	95	95	95

*Notes: The dependent variable is the 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.*

Table A2: Baseline Specification in First Differences

	(1)	(2)	(3)	(4)
5yr Total Debt	0.054*** (0.019)	0.050*** (0.018)	0.049*** (0.018)	0.049*** (0.018)
Dependent Variable	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$
Output Gap	t+1	t+1	t+5	t+1 - t+5
GDP Growth	t+5	t+5	t+5	t+5
Controls	×	×	×	×
Sample period	1987-2017	1987-2020	1987-2020	1987-2020
N	89	95	95	95

Notes: The dependent variable is the change in 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

Table A3: Primary Deficit and Forecast Horizon

	(1)	(2)	(3)	(4)	(5)	(6)
5yr Total Debt	0.049*** (0.018)	0.047*** (0.019)				
5yr Primary Debt			0.041** (0.021)	0.041** (0.021)		
10yr Primary Debt					0.014 (0.013)	0.010 (0.011)
Dependent Variable	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{5,10}$	$\Delta i_t^{10,10}$
Output Gap	t+1 - t+5	t+1 - t+5	t+1 - t+5	t+1 - t+5	t+1 - t+10	t+1 - t+10
GDP Growth	t+5	t+5	t+5	t+5	t+10	t+10
Controls	×	×	×	×	×	×
Sample period	1987-2020	1996-2020	1987-2020	1996-2020	1996-2020	1996-2020
N	95	68	95	68	68	68

Notes: The dependent variable is the change in 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

Table A4: Primary Deficit Components

	(1)	(2)
10yr Primary Debt	0.010 (0.011)	
10yr Revenues		0.018 (0.011)
10yr Mandatory		-0.082 (0.053)
10yr Discretionary		0.009 (0.025)
Dependent Variable	$\Delta_i^{10,10}$	$\Delta_i^{10,10}$
Output Gap	t+1 - t+10	t+1 - t+10
GDP Growth	t+10	t+10
Controls	×	×
Sample period	1996-2020	1996-2020
N	68	68

Notes: The dependent variable is the change in 5-year ahead 10-year forward interest rate. Standard errors in parentheses. * denotes significance at the 10% level, ** at the 5% level, and *** at the 1% level.

B Construction of the Balanced Growth Path

This appendix provides a formal construction of the Balanced Growth Path for the set of economies described in [Section 2](#). We construct the Balanced Growth Path in multiple parts. In [Appendix B.1](#), we construct the Balanced Growth Path for aggregates. In [Appendix B.2](#), we construct the Balanced Growth Path for individual agents' allocations. Finally, in [Appendix B.3](#), we put these elements together to characterize the balanced growth path for the distribution and the aggregation of households.

B.1 Aggregate Conditions

Balanced Growth Path: A Balanced Growth Path (BGP) is a sequence

$$\{C_t, A_t, Y_t, K_t, L_t, B_t, G_t, Tr_t\}_{t=0}^{\infty}$$

such that (i) for all $t = 0, 1, \dots$ $C_t, A_t, Y_t, K_t, B_t, G_t, Tr_t$ grow at a constant rate g_y ,

$$\frac{Y_{t+1}}{Y_t} = \frac{C_{t+1}}{C_t} = \frac{A_{t+1}}{A_t} = \frac{K_{t+1}}{K_t} = \frac{B_{t+1}}{B_t} = \frac{G_{t+1}}{G_t} = \frac{Tr_{t+1}}{Tr_t} = 1 + g_y$$

(ii) per capita variables all grow at the same constant rate g_w :

$$\frac{Y_{t+1}/N_{t+1}}{Y_t/N_t} = \frac{C_{t+1}/N_{t+1}}{C_t/N_t} = \frac{A_{t+1}/N_{t+1}}{A_t/N_t} = \frac{K_{t+1}/N_{t+1}}{K_t/N_t} = \frac{B_{t+1}/N_{t+1}}{B_t/N_t} = \frac{G_{t+1}/N_{t+1}}{G_t/N_t} = \frac{Tr_{t+1}/N_{t+1}}{Tr_t/N_t} = 1 + g_w$$

and (iii) effective labor per capita is constant:

$$\frac{L_{t+1}}{N_{t+1}} = \frac{L_t}{N_t} = \frac{L_0}{N_0}$$

Denote time 0 variables without a time subscript, for example $L \equiv L_0$.

Growth Rates: Let all growth derive from TFP $g_z > 0$ and population $g_n > 0$ growth. Then on a balanced growth path we assume:

$$Z_t = (1 + g_z)^t Z$$

$$N_t = (1 + g_n)^t N$$

where Z and N are steady state values. Then, from part (iii) of the definition, growth

in labor is:

$$\frac{L_{t+1}}{L_t} = \frac{L_{t+1}/N_{t+1}}{L_t/((1+g_n)N_t)} = 1 + g_n$$

In steady state $Y = ZK^\alpha L^{1-\alpha}$. Let output growth be given by $g_y > 0$. Therefore the production function gives:

$$Y_t = Z_t K_t^\alpha L_t^{1-\alpha} \implies (1 + g_y) = (1 + g_z)^{\frac{1}{1-\alpha}} (1 + g_n)$$

Lastly, from parts (ii) and (iii) of the Balanced Growth Path definition, we can solve for the growth of per capita variables:

$$\frac{Y_{t+1}/N_{t+1}}{Y_t/N_t} = \frac{Z_{t+1}}{Z_t} \left(\frac{K_{t+1}/N_{t+1}}{K_t/N_t} \right)^\alpha \left(\frac{L_{t+1}/N_{t+1}}{L_t/N_t} \right)^{1-\alpha} \implies (1 + g_w) = (1 + g_z)^{\frac{1}{1-\alpha}}$$

Prices: From Euler's theorem we know:

$$Y_t = \alpha Y_t + (1 - \alpha) Y_t = (r_t + \delta) K_t + w_t L_t$$

Accordingly, the wage and interest rate depend on the capital-labor ratio. Growth in the capital-labor ratio is:

$$\frac{K_{t+1}/L_{t+1}}{K_t/L_t} = (1 + g_z)^{\frac{1}{1-\alpha}} = 1 + g_w$$

Therefore, the growth rate for the wage is:

$$\frac{w_{t+1}}{w_t} = \frac{Z_{t+1}}{Z_t} \cdot \left(\frac{K_{t+1}/L_{t+1}}{K_t/L_t} \right)^\alpha = 1 + g_w$$

and the growth rate for the interest rate is:

$$\frac{r_{t+1} + \delta}{r_t + \delta} = \frac{Z_{t+1}}{Z_t} \cdot \left(\frac{K_{t+1}/L_{t+1}}{K_t/L_t} \right)^{\alpha-1} = 1$$

Therefore wages grow while interest rates do not.

Equilibrium Conditions: The detrended *asset market clearing condition* is:

$$K_t = A_t + F_t + B_t \implies K = A + F + B$$

The detrended *resource constraint* is:

$$C_t + K_{t+1} + G_t + Tr_t = Y_t + (1 - \delta)K_t \implies C + (g_y + \delta)K + G + Tr = Y$$

and the detrended *government budget constraint* is:

$$G_t + Tr_t + B_{t+1} - B_t = R_t + rB_t \implies G + Tr = R + (r - g_y)B$$

B.2 Individual Conditions

Preferences: We assume that labor disutility and utility over bequests have a time-dependent component. Specifically, we assume labor disutility grows at the same rate as the utility over consumption, such that $v_{t+1}(h, d) = (1 + g_w)^{1-\sigma} v_t(h, d)$. Therefore, total utility over consumption, hours and retirement status is:

$$u(c_t) - v_t(h_t, d_t) = \left[(1 + g_w)^{1-\sigma} \right]^t (u(c) - v(h, d)).$$

Similarly, assume that the non-homothetic component of the utility over bequests grows at the same rate as the utility over consumption, such that

$$\phi(a_{t+1}) = \left[(1 + g_w)^{1-\sigma} \right]^{t+1} \phi(a').$$

Bequests: Because bequest inflows $b_j(\kappa)$ are generated from the households' savings from the previous period, bequests grow at the same rate as savings.

Social Security: In order for the AIME to grow at the same rate as the wage, we assume a cost of living adjustment (COLA) on Social Security taxes and payments. For social security taxes, the cap on eligible income grows at the rate of wage growth, $\bar{m}_t = (1 + g_w)^t \bar{m}$. Furthermore, base payment bend points $b_{i,t}^{ss} = (1 + g_w)^t b_i^{ss}$ and base payment values $\tau_{r,i,t} = (1 + g_w)^t \tau_{r,i}$ for $i = 1, 2, 3$.

Medical Expenses and Policy: We assume that medical expenses are indexed to wage growth and so $\mu_t = (1 + g_w)^t \mu$ at all ages. We also assume that the consumption floor achieved by medical transfers, $\underline{c}_t$, also receives a COLA so that it grows at the same rate as the wage and therefore $\underline{c}_t = (1 + g_w)^t \underline{c}$. By construction, this implies that individuals' medical transfers also grow at the same rate as the wage, $Tr_t = (1 + g_w)^t Tr$.

Tax Function: On a Balanced Growth Path, (c_t, a'_{t+1}, a_t) and $\tilde{y}_t$ must all grow at the same rate as the wage. Furthermore, the tax function must grow at the same rate as the wage. Recalling the tax function, $Y_t(\tilde{y}_t)$, τ_2 must grow at the same rate as $\tilde{y}_t^{-\tau_1}$. Rewrite as:

$$Y_t(\tilde{y}_t) = \tau_0 \left((1 + g_w)^t \tilde{y} - [(1 + g_w)^t]^{-\tau_1} \tilde{y}^{-\tau_1} + [(1 + g_w)^t]^{-\tau_1} \tau_2 \right)^{-\frac{1}{\tau_1}} = (1 + g_w)^t Y(\tilde{y})$$

Individual Budget Constraint: Let the function $T(h, a, \varepsilon, m, d)$ contain income taxes, social security taxes or payments, medical expenses or transfers, and bequest inflows that a household faces. A household's time t budget constraint is:

$$c_t + a'_{t+1} \leq w_t \varepsilon_t h_t + (1 + r_t) a_t - T_t(h_t, a_t, \varepsilon_t, m_t, d_t)$$

$$c + (1 + g_w) a' \leq w \varepsilon h + (1 + r) a - T(h, a, \varepsilon, m, d)$$

where $\{c, a', a, h, w, r, \varepsilon\}$ are stationary variables. Given that the tax function $Y(\tilde{y})$ grows at rate g_w , so will the transfer function $T(h, a, \varepsilon)$ in the infinitely lived agent model. Furthermore, given that the Social Security program $\{\bar{m}, b_i^{ss}, \tau_{r,i}\}$, medical system $\{\underline{c}, Tr, \mu\}$ and bequest inflows $\{b(\kappa)\}$ grow at rate g_w , so will the transfer $T(h, a, \varepsilon, m, d)$ function in the life cycle model.

B.3 Aggregation

Distributions: For j -th cohort at time t , the measure over $(a, \varepsilon, m, d_{-1})$ is given by:

$$\begin{aligned} \lambda_{j,t}(a_t, \varepsilon, m_t, d_{-1}) &= \lambda_{j,t-1} \left(\frac{a_t}{1 + g_w}, \varepsilon, \frac{m_t}{1 + g_w}, d_{-1} \right) (1 + g_n) \\ &= \lambda_{j,t-i} \left(\frac{a_t}{(1 + g_w)^i}, \varepsilon, \frac{m_t}{(1 + g_w)^i}, d_{-1} \right) (1 + g_n)^i \quad \forall i \leq t \\ &= \lambda_j(a, \varepsilon, m, d_{-1}) N_{t-j+1}. \end{aligned}$$

Therefore, $\lambda_j(a, \varepsilon, m, d_{-1})$ is a stationary distribution over age j households that integrates to one.

Aggregation: Aggregate consumption in the life cycle model is constructed as follows.

Define the relative size of cohorts as $\omega_1 = 1$ and:

$$\omega_{j+1} = \frac{N_{t-j}}{N_t} \cdot \prod_{i=1}^j \psi_i = (1 + g_n)^{-j} \prod_{i=1}^j \psi_i = \frac{\psi_j \omega_j}{1 + g_n} \quad \forall j = 1, \dots, J-1$$

Let $C_{j,t}$ be aggregate consumption per age- j household, which is derived from the age- j household's allocation:

$$C_{j,t} = \int (1 + g_w)^t c_j(a, \varepsilon, m, d_{-1}) \mathbf{d}\lambda_j = (1 + g_w)^t \int c_j(a, \varepsilon, m, d_{-1}) \mathbf{d}\lambda_j = (1 + g_w)^t C_j$$

where C_j is the stationary aggregate consumption per age- j household. Accordingly, aggregate consumption is:

$$\begin{aligned} C_t &= N_t \left(C_{1,t} + \psi_1 (1 + g_n)^{-1} C_{2,t} + \dots + \left(\prod_{i=1}^{J-1} \psi_i \right) (1 + g_n)^{-(J-1)} C_{J,t} \right) \\ &= (1 + g_w)^t N_t \sum_{j=1}^J \omega_j C_j \\ &= (1 + g_y)^t C \end{aligned}$$

where C is the stationary level of aggregate consumption and where we have normalized $N = 1$.

We can similarly construct the remaining aggregates $\{A, K, Y, B, G\}$ on the balanced growth path. Notably, however, labor per capita does not grow. Aggregate labor per capita is constructed as:

$$L_t = N_t \sum_{j=1}^J \omega_j L_j \implies L = \frac{L_t}{N_t} = \sum_{j=1}^J \omega_j \int d_j(a, \varepsilon, m, d_{-1}) \varepsilon h_j(a, \varepsilon, m, d_{-1}) \mathbf{d}\lambda_j$$

which is the sum over ages of aggregate labor per age- j household.

C Calibration

In this appendix, we detail the construction of empirical measures that we feed into the model.

Demographics: To measure household survival rates from mortality tables, we account for demographic changes such as variation in the size of the household and

mortality rates by age and sex, and we define household mortality as when either both members of a married household die or when the sole remaining adult of a household dies. Accordingly, we construct the household-level mortality rate as,

$$\psi_j \equiv \omega_j^{single} \left[\omega_j^{male} \psi_j^{male} + (1 - \omega_j^{male}) \psi_j^{female} \right] + (1 - \omega_j^{single}) \psi_j^{male} \psi_j^{female},$$

where ψ_j^{male} and ψ_j^{female} are survival probabilities for age j males and females respectively, and $\omega_j^{single} \omega_j^{male}$ is the fraction of single-adult households with an age- j male head of household. We obtain mortality rates by age and sex from [Bell and Miller \(2002\)](#) and derive $\{\psi_j\}_{j=1}^{J-1}$ by applying a quartic polynomial in age to the raw series.

Preferences: We compute the adult equivalent scale at each age (of the head of household) to convert households of varying sizes into a standardized measure,

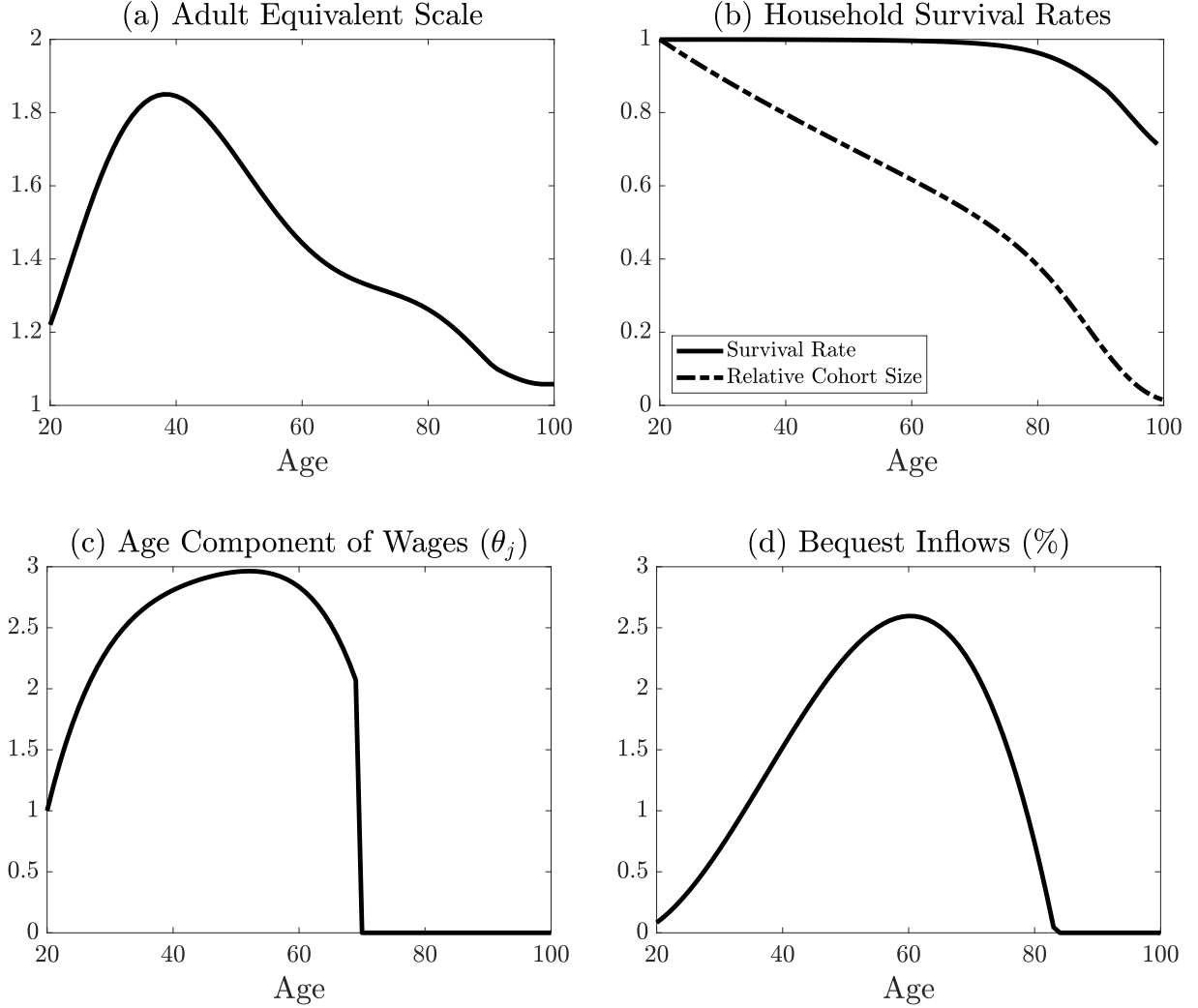
$$\tilde{n}_j \equiv \left[\omega_j^{single} \cdot 1 \right] + \left[(1 - \omega_j^{single}) \cdot 1.5 \right] + (1/3)n_j^c$$

where ω_j^{single} is the fraction of single-adult households with an age- j head of household, and n_j^c is the average number of children in a household with an age- j head of household. For each household in the 2007 Survey of Consumer Finances, we observe a head of household, a spouse (if there is one), and children (if there are any). We compute the share of single-adult households with an age- j head of household, denoted ω_j^{single} , and the share of married households with age- j head of household, given by $1 - \omega_j^{single}$. We derive $\{n_j\}_{j=1}^J$ by applying a quartic polynomial in age to the measured profile of $\{\tilde{n}_j\}_{j=1}^J$.

Bequests: When constructing the bequest distribution, we normalize the distribution by aggregate labor income. We use the HRS-AHEAD dataset, using estate inheritances and excluding intra-household bequests by dropping observations in which estates were transferred to a spouse. We use the CPI to convert to \$2002 and normalize by the Social Security's labor income adjustment (the 2002 Average Wage Index, <https://www.ssa.gov/oact/cola/awidevelop.html>).

The total level of bequests to type- κ households is determined by the total amount of wealth held by type- κ households upon death. For each type, these bequests are allocated to living households to match shares of bequests received by age in the Survey of Consumer Finances, according to the function $b_j(\kappa)$. In particular, we construct

Figure A1: Household Size, Mortality, Wage, and Bequest Profiles



the function $b_j(\kappa)$ from the relationship

$$(1 + g_n)b_j(\kappa) = \omega_j^b \cdot \sum_{j=1}^J \omega_j(1 - \psi_j) \int a'_j(a, \varepsilon, m, d_{-1}) d\lambda_j(a, \varepsilon, m, d_{-1}|\kappa)$$

which must hold for each household-type κ and age- j , and where $\{\omega_j^b\}_{j=1}^J$ are the shares of bequests received from the Survey of Consumer Finances, scaled by the total bequests by type- κ households in the model. To compute $\{\omega_j^b\}_{j=1}^J$, we take total household-level bequests by age from [Feiveson and Sabelhaus \(2018, 2019\)](#) and apply a quartic polynomial in age and normalize to convert to lifetime shares by age such that $\sum_{j=1}^J \omega_j^b = 1$.

Medical Expenditures: We compute medical expenditures at each age as the weighted average for single and married households, controlling for the household's composition of men and women. To do so, denote average medical expenditures for age- j men and women by μ_j^m and μ_j^f , respectively, and recall that ω_j^{single} and ω_j^{male} denote the share of single households and share of single households with a male head, respectively. Following [DeNardi, French, and Jones \(2010\)](#) and [Kopecky and Koreshkova \(2014\)](#), we compute out-of-pocket medical expenditures by sex and age (μ_j^m, μ_j^f) in the HRS-AHEAD dataset by regressing individual expenditures on a quartic polynomial in age and include individual-specific fixed effects in order to alleviate measurement error and survivorship bias. Accordingly, the average medical expenditures for a household with head of age- j are the weighted average of single male, single female and married household expenditures,

$$\tilde{\mu}_j = \omega_j^{single} \left[\omega_j^{male} \mu_j^m + (1 - \omega_j^{male}) \mu_j^f \right] + (1 - \omega_j^{single}) \left(\frac{1}{2} \mu_j^m + \frac{1}{2} \mu_j^f \right) .$$

We derive μ_j by applying a quartic polynomial in age to $\{\tilde{\mu}_j\}_{j=\bar{J}_{ret}}^J$.